## E OPTIMIST CLASSES IIT-JAM TOPPERS



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# CSIR-NET-JRF RESULTS 2022



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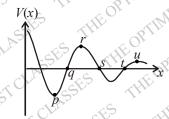
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- For the function  $\phi = x^2 y + xy$  the value of  $|\vec{\nabla} \phi|$  at x = y = 1 is

- (c) 13

- The avrage of the function in the interval is

- Identify the points of unstable equilibrium for the potential shown in the figure.



- (b) q and t

- Q4.  $W^{r}$ Which one of the following remains invariant under Lorentz transformations?

- A charge +q is kept at a distance of 2R from the centre of a grounded conducting sphere of radius R. The image charge and its distance from the centre are, respectively
- (c) -q and  $\frac{R}{2}$
- NSQ6. The state of polarization of light with the electric field vector  $\vec{E} = \hat{i}E_0 \cos(kz - iz)$ 
  - (a) Linearly polarized along z-direction
  - (b) Linearly polarized at -45° to x-axis
  - (c) Circularly polarized
  - (d) Elliptically polarized with the major axis along x-axis
  - The resonance widths  $\Gamma$  of  $\rho$ ,  $\omega$  and  $\varphi$  particle resonances satisfy the relation  $\Gamma_{\rho} > \Gamma_{\omega} > \Gamma_{\varphi}$ . Their life-

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	times satisfy the relation THE OF THE
THEORY	times satisfy the relation (a) $\tau_{\rho} > \tau_{\omega} > \tau_{\varphi}$ (b) $\tau_{\rho} < \tau_{\omega} < \tau_{\varphi}$ (c) $\tau_{\rho} = \tau_{\omega} = \tau_{\varphi}$ (d) $\tau_{\rho} > \tau_{\omega} < \tau_{\varphi}$ The time independent Schödinger equation of a system represents the conservation of the
STUE	$(a) \ \iota_{\rho} > \iota_{\omega} > \iota_{\varphi} \qquad (b) \ \iota_{\rho} < \iota_{\omega} < \iota_{\varphi} \qquad (c) \ \iota_{\rho} = \iota_{\omega} = \iota_{\varphi} \qquad (d) \ \iota_{\rho} > \iota_{\omega} < \iota_{\varphi}$
Q8.	The time independent Schödinger equation of a system represents the conservation of the  (a) total binding energy of the system.  (b) total potential energy of the system.
SSS	(c) total kinetic energy of the system. (d) total energy of the system.
CLASS Q9.5	In a hydrogen atom, the accidental or Coulomb degeneracy for the $n = 4$ state is
CLASS	(a) 4 (b) 16 (c) 18 (d) 32
MST GLAS	The Hamiltonian of a particle is given by $H = \frac{p^2}{2m} + V( \vec{r} ) + \phi( \vec{r} )\vec{L}\cdot\vec{S}$ where $\vec{S}$ is the spin, $V( \vec{r} )$ and
TMISTQ10.	(a) 4 (b) 16 (c) 18 (d) 32  The Hamiltonian of a particle is given by $H = \frac{p^2}{2m} + V( \vec{r} ) + \phi( \vec{r} ) \vec{L} \cdot \vec{S}$ where $\vec{S}$ is the spin, $V( \vec{r} )$ and
OLA Q9.5  MSTCHASSES  PIMISTQ10.	The Hamiltonian of a particle is given by $H = \frac{p^2}{2m} + V( \vec{r} ) + \phi( \vec{r} )\vec{L} \cdot \vec{S}$ where $\vec{S}$ is the spin, $V( \vec{r} )$ and $\phi( \vec{r} )$ are Potential functions and $\vec{L} = \vec{r} \times \vec{p}$ is the angular momentum. The Hamiltonian does NOT commute with  (a) $\vec{L} + \vec{S}$ (b) $\vec{S}^2$ (c) $\vec{L}_z$ (d) $\vec{L}^2$
E OP I	with LASSI IS THE OPTIME OPTIME OPTIME OPTIME OPTIME
THE OP'T	(a) $\vec{L} + \vec{S}$ (b) $\vec{S}^2$ OPTIMIST (c) $\vec{L}_z$ Set $\vec{L}_z$ (d) $\vec{L}^2$
QH.	The spectral terms for a certain electronic configuration are given by <sup>3</sup> D, <sup>1</sup> D, <sup>3</sup> P, <sup>1</sup> P, <sup>5</sup> S, <sup>3</sup> S. The term with the
The off	Plowest energy is:
,5° 71°	(a) <sup>3</sup> S (b) <sup>3</sup> P (c) <sup>3</sup> D (d) <sup>3</sup> S
Q12.	The degeneracy of the spectral term <sup>3</sup> F is:
CLASSI	(a) 7 (b) 9 (c) 15 (c) 15 (d) 21 (d) 21 (d) 21
Q13.	$\phi( \vec{r} )$ are Potential functions and $\vec{L} = \vec{r} \times \vec{p}$ is the angular momentum. The Hamiltonian does NOT commute with  (a) $\vec{L} + \vec{S}$ (b) $\vec{S}^2$ (c) $\vec{L}_2$ (d) $\vec{L}^2$ The spectral terms for a certain electronic configuration are given by $^3D$ , $^1D$ , $^3P$ , $^1P$ , $^5S$ , $^3S$ . The term with the lowest energy is:  (a) $^3S$ (b) $^3P$ (c) $^3D$ (d) $^3S$ The degeneracy of the spectral term $^3F$ is:  (a) $^7$ (b) $^9$ (c) $^1S$ (d) $^1S$ The Lande $g$ factor the level $^3D_3$ is:  (a) $\frac{2}{3}$ (b) $\frac{3}{2}$ (c) $\frac{3}{4}$ (d) $\frac{4}{3}$ All vibrations producing a change in the electric dipole moment of a molecule yield  (a) Raman spectra (b) Infrared spectra (c) Ultra-violet spectra (d) X-ray spectra.
(6)	(a) $\frac{2}{3}$ (b) $\frac{3}{3}$ (c) $\frac{3}{4}$ (c) $\frac{3}{4}$ (d) $\frac{4}{3}$ (e) $\frac{4}{3}$
Q14.	(a) $\frac{2}{3}$ (b) $\frac{3}{2}$ (c) $\frac{3}{4}$ (d) $\frac{1}{3}$ All vibrations producing a change in the electric dipole moment of a molecule yield  (a) Raman spectra (b) Infrared spectra (c) Ultra-violet spectra (d) X-ray spectra
OPTIONS	(a) Raman spectra (b) Infrared spectra (c) Ultra-violet spectra (d) X-ray spectra For any process, the second law of thermodynamics requires that the change of entropy of the universe be (a) positive only (b) positive or zero (c) zero only (d) negative or zero
PQ13.	(a) positive only (b) positive or zero (c) zero only (d) negative or zero
Q16.	The dimension of phase space of ten rigid diatomic molecules is (a) 5 (b) 10 (c) 50 (d) 100
Q17.	The specific heat of an ideal Fermi gas in 3-dimension at very low temperature (T) varies as
Q18.	
ASSICES	
CLAS Q19.	(c) Normal liquid He to superfluid He (d) Superconducting to normal state  The <i>c/a</i> ratio for an ideal hexagonal closed packed structure is
CLASS	(a) Vaporization of a liquid at its boiling point (b) Ferromagnetic to paramagnetic (c) Normal liquid He to superfluid He (d) Superconducting to normal state  The $c/a$ ratio for an ideal hexagonal closed packed structure is  (a) $2/\sqrt{3}$ (b) $\sqrt{8}$ (c) $\sqrt{5}$ (d) $\sqrt{8/3}$ The number of independent elastic constants in an isotropic cubic solid is  (a) 1 (b) 2 (c) 3 (d) 4  The effective mass of an electron in a semiconductor
Q20.5	The number of independent elastic constants in an isotropic cubic solid is  (a) 1 (b) 2 (c) 3 (d) 4
Q21.	The critical magnetic field for a solid in superconducting state  (a) $2/\sqrt{3}$ (b) $\sqrt{8}$ (c) $\sqrt{5}$ (d) $\sqrt{8/3}$ The number of independent elastic constants in an isotropic cubic solid is  (a) 1 (b) 2 (c) 3 (d) 4  The effective mass of an electron in a semiconductor  (a) can never be positive (b) can never be negative  (c) can be positive or negative (d) depends on its spin  The critical magnetic field for a solid in superconducting state
JP 1 TIMIST	The effective mass of an electron in a semiconductor  (a) can never be positive  (b) can never be negative  (c) can be positive or negative  (d) depends on its spin
Q22.1	(c) can be positive (d) depends on its spin  The critical magnetic field for a solid in superconducting state  (a) does not depend upon temperature  (b) can nevel be negative  (d) depends on its spin  The critical magnetic field for a solid in superconducting state  (b) increase if the temperature increases
THE OPTIME	(a) can never be positive (b) can never be negative (c) can be positive or negative (d) depends on its spin  The critical magnetic field for a solid in superconducting state (a) does not depend upon temperature (b) increase if the temperature increases (c) increases if the temperature decreases (d) does not depend on the transition temperature
TI. OP	(c) increases if the temperature decreases (d) does not depend on the transition temperature

S THE Q23	(a) mass number (c) neutron number	(b) Proton Number (d) electron number
Q24 SSES Q24	from about 8.8 MeV to 7.6 MeV. This trend is (a) short range nature of the nuclear force (c) tensor nature of the nuclear forces	o <sup>235</sup> U nucleus, the nuclear binding energy per particle decreases smainly due to the  (b) long range nature of the Coulomb forces  (d) spin dependence of the nuclear forces
Q25	. A thermal neutron having speed v impinges o	n a U <sup>235</sup> nucleus. The reaction cross-section is proportional to
MST C. AS	St(a) v-1 till	(c) $v^{1/2}$ Prime (d) $v^{-1/2}$
Q26	. Choose the particle with zero Baryon number	from the list given below
Print Q27		from the list given below (c) proton (d) $\Delta^{+}$ forward biased and either the collector or emitter open, operates
ill OPTIM	(a) cut-off region (b) saturation region	(c) pinch-off region (d) active region
THE Q28	(a) Unipolar device (c) Unijunction divice	(b) Special type of bipolar junction transistor. (d) device with low input impedance
JASSES Q29	being grounded. A voltage signal $v_i$ is applied configuration, the op-amp functions as (a) an open loop inverter	implifier (op-amp) is shorted with the output terminal apart from to the non-inverting input terminal of the op-amp. Under this  (b) a voltage to current converter  (d) an oscillator
IMIST Q30	<ul> <li>(c) a voltage follower</li> <li>A half-adder is a digital circuit with</li> <li>(a) Three inputs and one output</li> <li>(c) Two inputs and one output</li> </ul>	<ul><li>(b) a voltage to current converter</li><li>(d) an oscillator</li><li>(b) Three inputs and two outputs</li><li>(d) Two input and two outputs.</li></ul>
DTIMI.	Q. 31 - Q.90: Carry Two marks each.	CSES THEOR STIMIST CLASS SES THEORY
THE OPT		igenvalues -1 and +1. The other eigenvalues are: (c) zero and +2  (d) -1 and +1  (e) zero and +2  (d) -1 and +1  (e) $\frac{7}{25} - i\frac{24}{25}$ (d) $-\frac{7}{25} - i\frac{24}{25}$ (e) and elements (e) $\frac{7}{25} - i\frac{24}{25}$ (e) 4 $\pi$ for $a = 2$ (f) $\frac{\pi}{2}$ for $a = \frac{1}{2}$
Q32	The eigenvalues of the matrix $\begin{pmatrix} 1 & i \\ -i & 1 \end{pmatrix}$ are:	MIST CLASSES THE OF OPTIMIS UST CLASSES
SSES THE	(a) +1 and +1 (b) zero and +1	(c) zero and +2 (d) -1 and +1
A SQ33	The inverse of the complex number $\frac{3+4i}{3-4i}$ is	OF OPTIMIS ASSES THE OF OPTIMIST OF CLASS
MISTOLASSI	(a) $\frac{7}{25} + i\frac{24}{25}$ (b) $-\frac{7}{25} + i\frac{24}{25}$	(c) $\frac{7}{25} - i\frac{24}{25}$ (d) $-\frac{7}{25} - i\frac{24}{25}$
JETIMIS Q34	The value of $\int_{c} \frac{dz}{(z^2 + a^2)}$ , where C is a unit circ	ele (anti clockwise) centered at the origin in the complex z-  (c) $4\pi$ for $a = 2$ (d) $\frac{\pi}{2}$ for $a = \frac{1}{2}$
OPTIME	plan is: 151 THE OPTIME 151 CL	ASSES THE OPTIME TELL SSES THE
HE OPTH	(a) $\pi$ for $a = 2$ (b) zero for $a = \frac{1}{2}$	(c) $4\pi$ for $a=2$ (d) $\frac{\pi}{2}$ for $a=\frac{1}{2}$

The Laplace transform of  $f(t) = \sin \pi t is F(s) = \frac{\pi}{\left(s^2 + \pi^2\right)}$ , s > 0. Therefore, the Laplace transform of  $t \sin \pi t$  is:

(a)  $\frac{\pi}{s^2 \left(s^2 + \pi^2\right)}$  (b)  $\frac{2\pi}{s^2 \left(s^2 + \pi^2\right)^2}$  (c)  $\frac{2\pi s}{\left(s^2 + \pi^2\right)^2}$  (d)  $\frac{2\pi s}{\left(s^2 + \pi^2\right)^2}$ A periodic function f(x) = x for  $-\pi < x < \pi$  has the Fourier series representation  $f(x) = \sum_{n=1}^{\infty} \left(-\frac{2}{n}\right) (-1)^n \sin nx$ . Using this, one finds the sum  $\sum_{n=1}^{\infty} \frac{1}{n^2}$  to be

(a)  $2 \ln 2$  (b)  $\frac{\pi^2}{3}$  (c)  $\frac{\pi^2}{6}$  (d)  $\pi \ln 2$ 

(a) 
$$\frac{\pi}{s^2(s^2+\pi^2)}$$
 (b)  $\frac{2\pi}{s^2(s^2+\pi^2)^2}$  (c)  $\frac{2\pi s}{(s^2+\pi^2)^2}$  (d)  $\frac{2\pi s}{(s^2+\pi^2)^2}$ 

$$f(x) = \sum_{n=1}^{\infty} \left(-\frac{2}{n}\right) (-1)^n \sin nx$$
. Using this, one finds the sum  $\sum_{n=1}^{\infty} \frac{1}{n^2}$  to be

(d)  $\pi \ln 2$   $dx f^{m+1}$ The Fourier transform F(k) of a function f(x) is defined as  $F(k) = \int_{-\infty}^{\infty} dx f(x) \exp(ikx)$ . The F(k) for f(x)  $= \exp(-x^2) \text{ is : [Given : } \int_{-\infty}^{\infty} \exp(-x^2) dx = \sqrt{\pi} \text{ ]}$ (a)  $\pi \exp(-k)$  (b)  $\sqrt{\pi} \exp\left(\frac{-k^2}{4}\right)$  (c)  $\frac{\sqrt{\pi}}{2} \exp\left(\frac{-k^2}{2}\right)$  (d)  $\sqrt{2\pi} \exp\left(-k^2\right)$ 

= exp(-x<sup>2</sup>) is: [Given: 
$$\int_{-\infty}^{\infty} \exp(-x^2) dx = \sqrt{\pi}$$
]

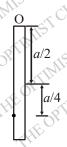
The Lagrangian of a particle moving in a plane under the influence of a central potential is given by

$$L = \frac{1}{2}m(\dot{r}^2 + r^2\dot{\theta}^2) - V(r)$$

The generalized momenta corresponding to r and  $\theta$  are given by

- (a)  $m\dot{r}$  and  $mr^2\dot{\theta}$
- (b)  $m\dot{r}$  and  $mr\dot{\theta}$  (c)  $m\dot{r}^2$  and  $mr^2\dot{\theta}$
- (d)  $m\dot{r}^2$  and  $mr^2\dot{\theta}^2$

Q39. A particle of mass m is attached to a thin uniform rod of length a and mass 4m. The distance of the particle from the center of mass of the rod is a/4. The moment of inertia of the combination about an axis passing through O normal to the rod is



A rigid frictionless rod rotates anticlock wise in a vertical plane with angular velocity  $\vec{\omega}$ . A bead of mass mmoves outward along the rod with constant velocity  $\vec{u}_0$ . The bead will experience a coriolis force

- (a)  $2mu_0\omega\hat{\theta}$
- (b)  $-2mu_0\omega\hat{\theta}$
- (c)  $4mu_0\omega\hat{\theta}$

Q41. The Hamiltonian corresponding to the Langragian  $L = a\dot{x}^2 + b\dot{y}^2$ 

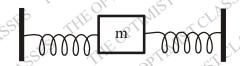
(a) 
$$\frac{p_x^2}{2a} + \frac{p_y^2}{2b} + kxy$$
 (b)  $\frac{p_x^2}{4a} + \frac{p_y^2}{4b} - kxy$  (c)  $\frac{p_x^2}{4a} + \frac{p_y^2}{4b} + kxy$  (d)  $\frac{p_x^2 + p_y^2}{4ab} + kxy$ 

- Q42. The value of the Poisson bracket  $\begin{bmatrix} \vec{a} \cdot \vec{r}, \vec{b} \cdot \vec{p} \end{bmatrix}$ , where  $\vec{a}$  and  $\vec{b}$  are constant vectors, is

- A mass m is connected on either side with a spring each of spring constant  $k_1$  and  $k_2$ . The free ends of springs are tied to rigid supports, The displacement of the mass is x from equilibrium position. Which one of the following is TRUE?
  - (a) The force acting on the mass is  $-(k_1k_2)^{1/2}x$
  - (b) The angular momentum of the mass is zero about the equilibrium point and its Lagrangian is

$$\frac{1}{2}m\dot{x}^2 - \frac{1}{2}(k_1 + k_2)x^2$$

(c) The total energy of the system is  $\frac{1}{2}m\dot{x}^2$ 



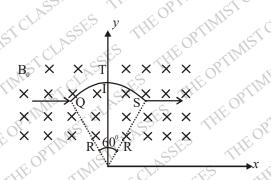
- (d) The angular momentum of the mass is  $mx\dot{x}$  and the Lagrangian of the system is  $\frac{m}{2}\dot{x}^2 + \frac{1}{2}(k_1)$
- An electron gains energy so that its mass becomes  $2m_0$ . Its speed is

- A conducting sphere of radius R has charge +Q on its surface. If the charge on the sphere is doubled and its radius is halved, the energy associated with the electric field will
  - (a) increase four times

(b) increase eight times

(c) remain the same

- (d) decrease four times
- A conducting sphere of radius R is placed in a uniform electric field  $\vec{E}_0$  directed along +z axis. The electric potential for outside points is given as  $V_{out} = -E_0 \left( 1 - \frac{R^3}{r^3} \right) r \cos \theta$ , where r is the distance from the centre and
  - $\theta$  is the polar angle. The charge density on the surface of the sphere is
- (b)  $\varepsilon_0 E_0 \cos \theta$  (c)  $3\varepsilon_0 E_0 \cos \theta$
- (d)  $\frac{\mathcal{E}_0}{3} E_0 \cos \theta$
- A circular arc QTS is kept in an external magnetic field  $\vec{B}_0$  as shown in figure. The arc carries a current I. The magnetic field is directed normal and into the page. The force acting on the arc is:



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(0)	n T	ח	n	
(a)	71	ĸ	ĸ	1
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(b) 
$$IB_0R\hat{j}$$

(c) 
$$-2IB_0R\hat{j}$$

(d) 
$$-IB_0R\hat{j}$$

A plane electromagnetic wave of frequency  $\omega$  is incident on an air-dielectric interface. The dielectric is linear, isotropic, non-magnetic and its refractive index is n. The reflectance (R) and transmittance (T) from the interface are

(a) 
$$R = \left(\frac{n-1}{n+1}\right)^2, T = \frac{4n}{(n+1)^2}$$

(b) 
$$R = -\left(\frac{n-1}{n+1}\right), T = \frac{2}{(n+1)^2}$$

(c) 
$$R = -\left(\frac{n-1}{n+1}\right)^3, T = \frac{4n^3}{(n+1)^2}$$

face are

(a) 
$$R = \left(\frac{n-1}{n+1}\right)^2$$
,  $T = \frac{4n}{(n+1)^2}$ 

(b)  $R = -\left(\frac{n-1}{n+1}\right)$ ,  $T = \frac{2}{(n+1)^2}$ 

(c)  $R = -\left(\frac{n-1}{n+1}\right)^3$ ,  $T = \frac{4n^3}{(n+1)^2}$ 

(d)  $R = -\left(\frac{n-1^2}{n+1}\right)$ ,  $T = \frac{4n^2}{(n+1)^2}$ 

- The electric field of a plane e.m. wave is  $\vec{E} = \vec{E}_0 \exp[i(xk\cos\alpha + yk\sin\alpha \omega t)]$ . If  $\hat{x}, \hat{y}$  and  $\hat{z}$  are cartesian unit vectors, the wave vector  $\hat{k}$  of the e.m. wave is

(b)  $\hat{x}k\sin\alpha + \hat{y}k\cos\alpha$ 

(c)  $\hat{x}k\cos\alpha + \hat{y}k\sin\alpha$ 

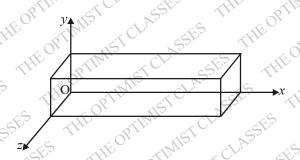
- The dispersion relation for a low density plasma is  $\omega^2 = \omega_0^2 + c^2 k^2$ , where  $\omega_0$  is the plasma frequency and cis the speed of light in free space. The relationship between the group velocity  $(v_g)$  and phase velocity is
  - (a)  $v_p = v$
- $(c) v_p v_g = c^2$
- (d)  $v_g = v_n^{1/2}$
- A Michelson interferometer is illuminated with monochromatic light, When one of the mirrors is moved through a distance 25.3  $\mu m$ , 92 fringes pass through the cross-wire. The wavelength of the monochromatic light is (a) 500 nm (d) 650 nm (b) 550nm (c) 600 nm
- A beam of monoenergetic particles having speed v is described by the wave function  $\psi(x) = u(x) \exp(ikz)$ where u(x) is a real function. This corresponds to a current density (a)  $u^2(x)v$ (d)  $u^2(x)$ (c) zero
- The wave function of a spin-less particle of mass m in a one-dimensional potential V(x) is  $\psi(x) = A \exp(-\alpha^2 x^2)$  corresponding to an eigenvalue  $E_0 = \hbar^2 \alpha^2 / m$ . The potential V(x) is
  - (a)  $2E_0(1-\alpha^2x^2)$  (b)  $2E_0(1+\alpha^2x^2)$  (c)  $2E_0\alpha^2x^2$  (d)  $2E_0(1+2\alpha^2x^2)$

- Two spin  $\vec{S}_1$  and  $\vec{S}_2$  interact via a potential  $V(r) = \vec{S}_1, \vec{S}_2 V_0(r)$ . The contributions of this potential in the (b)  $\frac{1}{2}V_0(r)$  and  $\frac{3}{2}V_0(r)$   $\frac{3}{2}V_0(r)$ singlet and triplet states, respectivley, are

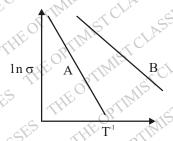
- and  $\frac{3}{2}V_0(r)$  and  $\frac{1}{4}V_0(r)$  on all harmonic  $(c) \frac{1}{4}V_0(r) \text{ and } -\frac{3}{4}V_0(r)$ Q55. The w 5. The wave function of a one-dimensional harmonic oscillator is  $\psi_0 = A \exp\left(\frac{-\alpha^2 x^2}{2}\right)$  for the ground state  $E_0 = \frac{\hbar \omega}{2}$ , where  $\alpha^2 = \frac{mw}{2}$  In the
  - $\frac{\hbar\omega}{2}$ , where  $\alpha^2 = \frac{mw}{\hbar}$ . In the presence of a perturbing of  $E_0 \left(\frac{\alpha x}{10}\right)^4$ , the first order change in the



with negative polarity at y = 0 plane. The sign and concentration of the majority charge carrier are, respec-



- (a) positive and  $5.2 \times 10^{19}$  m<sup>-3</sup>
- (b) negative and  $5.2 \times 10^{19} \,\text{m}^{-3}$
- (c) positive and  $10.4 \times 10^{19}$  m<sup>-3</sup>
- (d) negative and  $10.4 \times 10^{19}$  m<sup>-3</sup> ure
- Q65. The temperature dependence of the electrical conductivity  $\sigma$  of two intrinsic semiconductor A and B is shown in the figure. If  $E_A$  and  $E_B$  are the band gaps of A and B respectively, which one of the following is TRUE?



(a)  $E_A > E_B$ 

(b)  $E < E_{-}$ 

(c)  $E_A = E_B$ 

- (d)  $E_A$  and  $E_B$  both depend on temperature
- Q66. If the static dielectric constant of NaC1 crystal is 5.6 and its optical refractive index is 1.5, the ratio of its electric polarizability to its total polarizability is
  - (a) 0.5
- (b) 0.7
- (c) 0.8
- (d) 0.9

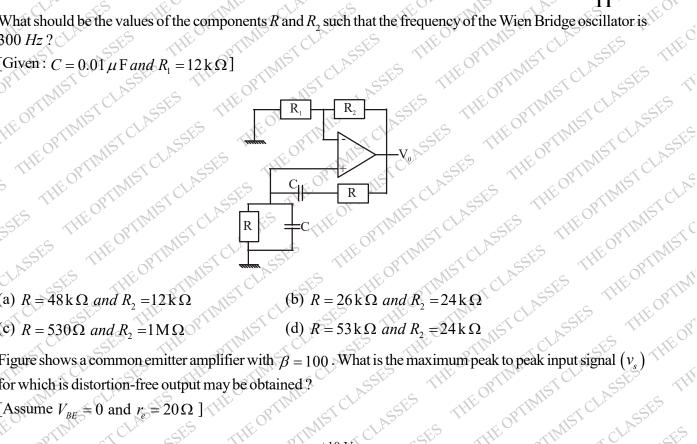
- Q67. Which one of the following statements is TRUE?
  - (a) Magnetic tapes are made of Iron
  - (b) Permanent magnets are made from ferrites
  - (c) Ultrasonic transducers are made from quartz crystals
  - (d) Optoelectronical devices are made from soft ferrites
- Q68. Which one of the following statements is NOT TRUE?
  - (a) Entropy decreases markedly on cooling a superconductor below the critical temperature,  $T_{\rm C}$
  - (b) The electronic contribution to the heat capacity in the superconducting state has an expontential form with an argument proportional to  $T^{-1}$ . suggestive of an energy gap
  - (c) A type I superconductor is a perfect diamagnet
  - (d) Critical temperature of superconductor does not vary with the isotopic mass
- Q69. The form factor  $F(\vec{q}) = \int \exp\left(i\vec{q}\cdot\frac{\vec{r}}{\hbar}\right)\rho(\vec{r})d^3r$  of Rutherford scattering is obtained by choosing a delta

function for the charge density  $\, 
ho(ec{r}) \,$  . The value of the form factor is

- (a) unity
- (b) infinity
- (c) zero
- (d) undefined
- Q70. Deuteron in its ground state has a total angular momentum J=1 and a positive parity. The corresponding orbital angular momentum L and spin S combination are
  - (a) L = 0, S = 1 and L = 2, S = 0
- (b) L = 0, S = 1 and L = 1, S = 1
- (c) L = 0, S = 1 and L = 2, S = 1
- (d) L = 1, S = 1 and L = 2, S = 1
- Q71. Which one of the following reactions is allowed?
  - (a)  $p \rightarrow n + e^{-1}$
- (b)  $p \rightarrow e^+ + v$
- (c)  $p \rightarrow \pi^+ + \gamma$
- (d)  $\overline{p} + n \rightarrow \pi^- + \pi^0$

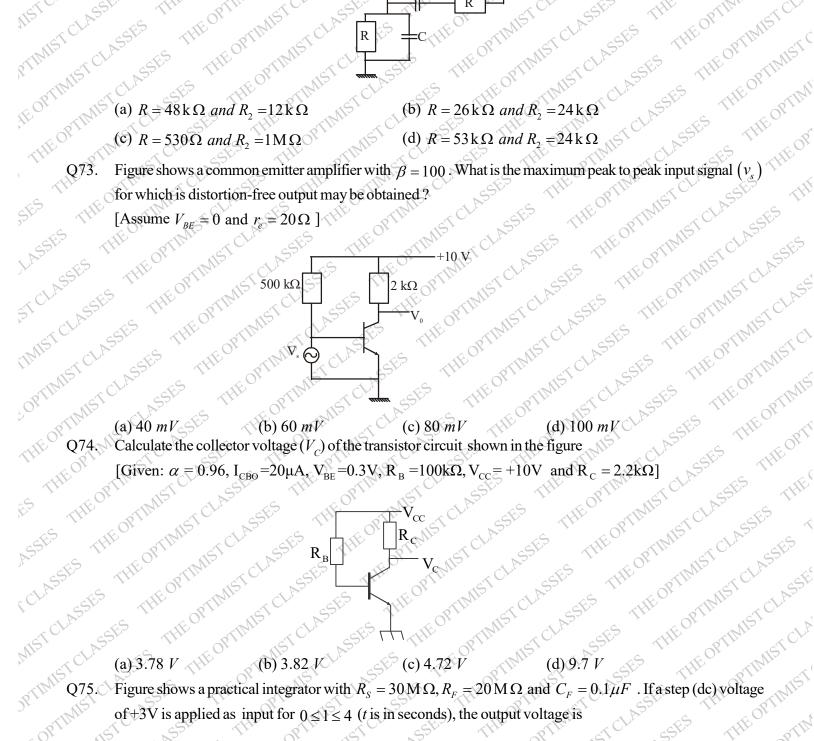
## 233, FIRST FLOOR, LAXMI NAGAR DELHI-110092

What should be the values of the components R and  $R_2$  such that the frequency of the Wien Bridge oscillator is  $300 \, Hz$ ? [Given:  $C = 0.01 \mu \text{ F}$  and  $R_1 = 12 \text{ k}\Omega$ ]

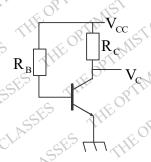


- $\text{TOK}\,\Omega \text{ and } R_2 = 12\,\text{k}\,\Omega$ (c)  $R = 530\,\Omega$  and  $R_2 = 1\,\text{M}\,\Omega$  Q73. Figure shows a commfor which is distortion-free output may be obtained?

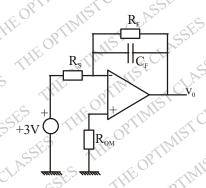
  [Assume V |  $\Omega$



(d) 100 mV CLASSES THE OPTIMIST CLASSES.



- $\frac{2.2 \text{k}\Omega}{\text{s}}$   $\frac{1.2 \text$ SPITMIST CLASSES THE OPTIMIST CLASSES (a)  $3.78 \ V$  (b)  $3.82 \ V$  (c)  $4.72 \ V$  (d)  $9.7 \ V$ Q75. Figure shows a practical integrator with  $R_S = 30 \ M \ \Omega$ ,  $R_F = 20 \ M \ \Omega$  and  $C_F = 0.1 \ \mu F$ . If a step (dc) voltage of  $+3 \ V$  is applied as input for  $0 \le 1 \le 4$  (t is in seconds), the output voltage is  $\frac{233, \text{ FIRST FIRST}}{CALL C}$



(a) a ramp function of -6 V

THE OPTIMIST CLASSES

(b) a step function of -12V

(c) a ramp function of -15V

- (d) a ramp function of -4V
- The Boolean expression  $Y = \overline{ABC}D + \overline{AB}CD + \overline{A}B\overline{C}D + \overline{A}B\overline{C}D$  reduces to
  - (a)  $\overline{A}B$
- (b) D

THE OPTIMIST CLAS

## Common Data for Q, 77 and Q. 78

Consider the differential equation y'' + p(x)y' + q(x)y(x) = 0.

Q77. If xp(x) and  $x^2q(x)$  have the Taylor series expansions

$$xp(x) = 4 + x + x^2 + \dots$$

$$x^2q(x) = 2 + 3x + 5x^2 + ...$$

then the roots of the incidicial equation are  $(a) - 1 \cdot 0$ 

- (a) 1, 0
- (b) -1, -2

If p(x) = 0 with the Wronskian at x = 0 as W(x = 0) = 1 and one of the solution is x, then the other linearly independent solution which vanishes at x = 1/2 is

- (b)  $1-4x^2$
- (c)x

## Common Data for Q. 79 and Q. 80

Consider a comet of mass m moving in a parabolic orbit around the Sun. The closest distance between the comet and the Sun is b, the mass of the Sun is M and the universal gravitation constant is G.

- The angular momentum of the comet is
- (b)  $b\sqrt{GmM}$
- (c)  $G\sqrt{mMb}$
- (d)  $m\sqrt{2GMb}$
- Q80. Wh:  $\frac{1}{2}$ Which one of the following is TRUE for the above system?
  - (a) The acceleration of the comet is maximum when it is closest to the Sun
  - (b) The linear momentum of the comet is a constant
  - (c) The comet will return to the solar system after a specified period
  - (d) The kinetic energy of the comet is a constant

Common Data for Q.81 and Q.82

Let  $\vec{E} = \hat{x}E_0 \exp\left[i\hat{k}\cdot\vec{r} - \omega t\right]$ , where  $\vec{k} = \hat{z}(k\cos\phi + ik\sin\phi)$ ,  $k = 1\vec{k}$  and  $\hat{x}$ ,  $\hat{y}$  and  $\hat{z}$  are cartesian unit vec-

tors, represent an electric field of a plane electro magnetic wave of frequency  $\omega$ 

- Which one of the following statements is TRUE?
  - (a) The magnitude of the electric field is attenuated as the wave propagates
  - (b) The energy of the e.m. wave flows along the x-direction
  - (c) The magnitude of the electric field of the wave is a constant
  - (d) The speed of the wave is the same as c (speed of light in free space)

## 233, FIRST FLOOR, LAXMI NAGAR DELHI-110092

(a) 
$$\hat{y} \frac{k}{\omega} E_0 \exp(-zk\sin\phi) \exp[i(zk\cos\phi - \omega t)]$$

The magnetic field 
$$\vec{B}$$
 of the wave is:

(a)  $\hat{y} \frac{k}{\omega} E_0 \exp\left(-zk\sin\phi\right) \exp\left[i(zk\cos\phi - \omega t)\right]$ 

(b)  $\hat{y} \frac{k}{\omega} E_0 \exp\left(-zk\sin\phi\right) \exp\left[i(zk\cos\phi - \omega t + \phi)\right]$ 

(c)  $\hat{y} \frac{k}{\omega} E_0 \exp\left[i(zk\cos\phi - \omega t + \phi)\right]$ 

(d)  $\hat{y} \frac{k}{\omega} E_0 \exp\left(-zk\cos\phi\right) \exp\left[i(zk\cos\phi - \omega t)\right]$ 

Common data for Q.83 and Q.84

A particle is confined to the region  $0 < x < L$  in one dimension.

If the particle is in the first excited state, then the probability of finding the particle is maximum at (a)  $x = \frac{L}{4}$  (b)  $x = \frac{L}{2}$  (c)  $x = \frac{L}{2}$  (d)  $x = \frac{L}{4}$  and  $\frac{3L}{4}$ 

(c) 
$$\hat{y} \frac{k}{\omega} E_0 \exp \left[ i \left( zk \cos \phi - \omega t + \phi \right) \right]$$

(c) 
$$y = E_0 \exp[1(2k\cos\phi - \omega t + \phi)]$$
  
(d)  $\hat{y} \frac{k}{\omega} E_0 \exp(-zk\cos\phi) \exp[i(zk\cos\phi - \omega t)]$   
Common data for Q.83 and Q.84  
A particle is confined to the region  $0 < x < L$  in one dimension.  
Q83. If the particle is in the first excited state, then the probability of finding the particle is maximum.  
(a)  $x = \frac{L}{6}$  (b)  $x = \frac{L}{2}$  (c)  $x = \frac{L}{3}$  (d)  $x = \frac{L}{4}$  and

(a) 
$$x = \frac{L}{6}$$

(b) 
$$x = \frac{L}{2}$$

(c) 
$$x = \frac{L}{3}$$

(d) 
$$x = \frac{L}{4}$$
 and  $\frac{3L}{4}$ 

 $x_{\perp}(zk\cos\phi - \omega t)$   $x_{\perp}(zk\cos\phi - \omega t)$ A particle is confined to the region 0 < x < L in one dimension.

If the particle is in the first excited state, then the probability of finding the particle is maximum at (a)  $x = \frac{L}{6}$  (b)  $x = \frac{L}{2}$  (c)  $x = \frac{L}{3}$  (d)  $x = \frac{L}{4}$  and  $\frac{3L}{4}$ .

If the particle is in the lowest energy state, then the probability of first excited state, the probability of first excited state, the probability of first excited state, the probability excited state, the probability excited state, the probability excited state, the probability excited state, the pr If the particle is in the lowest energy state, then the probability of finding the particle in the region  $0 < x < \frac{L}{4}$  is:

(a)  $\frac{1}{4} - \frac{1}{(2\pi)}$  (b)  $\frac{1}{4}$  (c)  $\frac{1}{4} + \frac{1}{(2\pi)}$  (d)  $\frac{1}{2}$ Common data for Q.85 and Q.86

The one-electron states for non-interacting electrons.  $(1/4)^{-1}$ 

(a) 
$$\frac{1}{4} - \frac{1}{(2\pi)}$$

(b) 
$$\frac{1}{4}$$

(c) 
$$\frac{1}{4} + \frac{1}{(2\pi)}$$

$$(d)\frac{1}{2}$$

Common data for Q.85 and Q.86

The one-electron states for norm. Q85. The energy of the lowest state is:

(b) 
$$\frac{\hbar^2 \pi^2}{2ma^2}$$

(c) 
$$\frac{\hbar^2 \pi^2}{ma^2}$$

$$(d) \frac{3\hbar^2 \pi^2}{2ma^2}$$

The one-electron states for non-interacting electrons confined in a cubic box of side a are  $\varepsilon_0 < \varepsilon_1 < \varepsilon_2 < \varepsilon_3 < \varepsilon_4$  etc.

5. The energy of the lowest state is:

(a) zero
(b)  $\frac{\hbar^2 \pi^2}{2ma^2}$ (c)  $\frac{\hbar^2 \pi^2}{ma^2}$ (d)  $\frac{3\hbar^2 \pi^2}{2ma^2}$ 5. The degeneracy (including spin) of the level  $\varepsilon_3$  is
(a) 2
(b) 4
(c) 6
(d) 8

Common data for Q.87 and Q.88

An ensemble of N three-level systems with energies  $\varepsilon = -\varepsilon_0$ ,  $0, +\varepsilon_0$  is in thermal equilibrium at temperature T. Let  $\beta = (k_B T)^{-1}$ If  $\beta \varepsilon_0 = 2$ , the probability of finding the system in the level  $\varepsilon - 0$  is:
(a)  $(\cos h 2)/2$ (d)  $(1+2\cos h 2)^{-1}$ 1) is approximate.

- $(c) \left(2\cosh 2\right)^{-1}$

Q88. The free energy of the system  $(a) (\cosh 2)/2$  (b)  $(\cosh 2)^{-1}$ The free energy of the system at high temperature (i.e.,  $x = \beta \varepsilon_0 << 1$ ) is approximately

- (b)  $-Nk_BT[\ln 2 + x^2/2]$ (d)  $-Nk_BT$
- $(c) -Nk_BT[\ln 3 + x^2/3]$

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Q89. The single particle	states occupied by the	last proton and the last n	eutron, respectively, are	given by	T
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