# E OPTIMIST CLASSES



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# CSIR-NET-JRF RESULTS 2022



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-JAM/JEST/TIFR/M.Sc ENTRANCE EXAMS

# GATE PAPER 2012

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	TON THE THE CONTRACTOR OF THE THIRD
	TON -IA OPTIMIST CLASSES THE OPTIMIST CLASSES THE OPTIMIST OF
Q1. Choose the grammatically INCORRECT senten	cett the prime and set the south
(a) They gave us the money back less the service	
(b) This country's expenditure is not less than of	Bangladesh
(d) This country's expenditure on educational rel	f Fifty Lakh rupees, but later settled for a lesser sum
Q2. Which one of the following options is the closest	in meaning to the word given below?
Mitigate Mitigate	in incaming to the word given ociow:
(a) Diminish (b) Divulge	(c) Dedicate (d) Denote
O3 Choose the most appropriate alternative from the	e options given below to complete the following sentence:
	eeded in its attempt to resolve the conflict
	(c) Meetings (d) Delegations
	by $5q^2$ , where q is the amount of production. The firm can
	nit. The number of units to be produced by the firm such
that the profit is maximized is	The spile of Co. Fight Lift still still still
(a) 5 (b) 10 (c)	(c) 15 HE OF TIMES (d) 25 AS SES THE OF TIMES
Q5. Choose the most appropriate alternative from the	e options given below to complete the following sentence
Suresh's dog is the one was hurt i	othe stamped
(a) that (b) which	(c) who (d) whom
Carry Two marks each	The is it of which chase is it of
Q6. Which of the following assertions are CORREC	17 SSL LIN OBLIL ISLO SSL THE
P: Adding / to each entry in a list adds / to the n	nean of the list
Q: Adding / to each entry in a list adds / to the s	rean of the list tandard deviation of the list of the list deviation of the list unchanged (c) P, R (d) R, S sorbers from two suppliers X and Y. X supplies 60% and Y absorbers are subjected to a quality test. The ones that X's shock absorbers, 96% are reliable, of Y's shock
S: Doubing each entry in a list looyee the standar	d deviation of the list unchanged
3. Dodding each entry in a list leaves the standard	(c) P. R. (d) R. S.
Q7. An automobile plant contracted to buy shock ab	sorbers from two suppliers X and Y. X supplies 60% and Y
supplies 40% of the shock absorbers. All shock	absorbers are subjected to a quality test. The ones that
pass the quality test are considered reliable. Of	X's shock absorbers, 96% are reliable. of Y's shock
absorbers, 72% are reliable.	THE OF TIMES CLAR SES THEOR TIMES , CLA
The probability that a randomly chosen shock at	osorber, which is found to be reliable, is made by Y is
(a) 0.288 (b) 0.334	(c) 0.667 (d) 0.720 (d)
	o the ground in which the annual convention is being held.
The profile of the arch follows the equaiton $y =$	$2x - 0.1x^2$ where y is the height of the arch in meters. The
maximum possible height of the arch is	ASSI THE OPTIME ISTON SSEL THE POINT
(a) 8 meters (b) 10 meters	(c) 12 meters (d) 14 meters
Q9. Wanted Temporary, Part-time persons for the	ne post of Field Interviewer to conduct personal
OPI USIC ASST THE OPILE OF	I' SSV THE OPTH STONESSE THE

233, FIRST FLOOR, LAXMI NAGAR DELHI-110092 CALL@ 09871044043 www.theoptimistclasses.com Email: info@theoptimistclasses.com interviews to collect economic data. Requirements: High School-pass, must be available for Day, Evening and Saturday work. Transportation paid, expenses reimbursed. Which one of the following is the best inference from the above advertisement?

(a) Gender-discriminatory

(b) Xenophobic

(c) Not designed to make the post attractive

(d) Not gender-discriminatory

Q10. Given the sequence of terms, AD CG FK JP, the next term is

# SECTION - B

# Q.1 - Q.25 : Carry ONE mark each.

Identify the CORECT statement for the following vectors  $\vec{a} = 3\hat{i} + 2\hat{j}$  and  $\vec{b} = \vec{a}$ (a) The vectors  $\vec{a}$  and  $\vec{b}$  are linearly independent (b) The vectors  $\vec{a}$  and  $\vec{b}$  are linearly dependent

(c) The vectors  $\vec{a}$  and b are orthogonal

(d) The vectors  $\vec{a}$  and  $\vec{b}$  are normalized

Two uniform thin rods of equal length L, and masses  $M_1$  and  $M_2$  are joined together along the length. The moment of inertia of the combined rod of length 2L about an axis passing through the mid-point perpendicular to the length of the rod is,

(a)  $(M_1 + M_2)\frac{L^2}{12}$  (b)  $(M_1 + M_2)\frac{L^2}{6}$  (c)  $(M_1 + M_2)\frac{L^2}{3}$  (d)  $(M_1 + M_2)\frac{L^2}{2}$ 

The space-time dependence of the electric field of a linearly polarized light in free space is given by where  $\hat{x}E_0\cos(\omega t-kz)$  where  $E_0,\omega$  and k are the amplitude, the angular frequency and the wavevector, respectively. The time averaged energy density associated with the electric field is

(a)  $\frac{1}{4} \varepsilon_0 E_0^2$ 

(d)  $2\varepsilon_0 E_0^2$ 

If the peak output voltage of a full wave rectifier is 10 V, its d.c. voltage is

(b) 7.07 V

(c) 6.36 V

(d) 3.18 V

Q5. A particle of masss m is confined in a two dimensional square well potential of dimension a. This potential V(x,y) is given by

$$V(x,y) = 0 \text{ for } -a < x < a \text{ and } -a < y < a$$
$$= \infty \text{ elsewhere}$$

The energy of the first excited state for this particle is given by,

(b)  $\frac{2\pi^2\hbar^2}{ma^2}$ 

(c)  $\frac{5\pi^2\hbar^2}{ma^2}$  (d)  $\frac{4\pi^2\hbar^2}{ma^2}$  as at temperature TThe isothermal compressibility,  $\kappa$  of an ideal gas at temperature  $T_0$  and volume  $V_0$ , is given by

(a)  $-\frac{1}{V_0} \frac{\partial V}{\partial P}\Big|_{T_0}$ (b)  $\frac{1}{V_0} \frac{\partial V}{\partial P}\Big|_{T_0}$ (c)  $-V_0 \frac{\partial P}{\partial V}\Big|_{T_0}$ (d)  $V_0 \frac{\partial P}{\partial V}\Big|_{T_0}$ 

The ground state of sodium atom  $\binom{11}{Na}$  is a  $^2S_{1/2}$  state. The difference in energy levels arising in the presence

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OPIL	of a weak external magnetic field $B$ , given in terms of Bohr magneton, $\mu_B$ is  (a) $\mu_B B$ (b) $2\mu_B B$ (c) $4\mu_B B$ (d) $6\mu_B B$ For an ideal Fermi gas in three dimensions, the electron velocity $V$ , at the Fermi surface is related to	~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~
THE OP	(a) $\mu_B B$ (b) $2\mu_B B$ (c) $4\mu_B B$ (d) $6\mu_B B$	SSEL
Q8.	THE STATE OF SES STEED, STATE STATES STEED, STATES	o electroi
ED .	concentration $n$ as  (a) $V_F \propto n^{2/3}$ (b) $V_E \propto n$ (c) $V_F \propto n^{1/2}$ (d) $V_F \propto n^{1/3}$	CLA
Q9,5 A55,5	(a) proton electron and neutron (b) proton, electron and photon (c) electron, photon and neutrino (d) quark, electron and meson	ATIMIST.
Q10.	In case of a Geiger-Muller (GM) counter, which one of the following statements is <b>CORRECT</b> ?  (a) Multiplication factor of the detector is of the order of 10 <sup>10</sup> .  (b) Type of the particles detected can be identified.  (c) Energy of the particles detected can be distinguished.  (d) Operating voltage of the detector is few tens of Volts.	THE OPTIM
Q11.	A palne electromagnetic wave travelling in free space is inincident normally on a glass plate of refract 3/2. If there is no absorption by the glass, its reflectivity is  (a) 4%  (b) 16%  (c) 20%  (d) 50%	tive index
Q12.	A Ge semiconductor is doped with acceptor impurity concentration of 10 <sup>15</sup> atoms/cm <sup>3</sup> . For the g	iven hol
	mobility of $1800  cm^3 / V - s$ , the resistivity of this material is:	CLAS
SSES	(a) $0.288\Omega cm$ (b) $0.694\Omega cm$ (c) $3.472\Omega cm$ (d) $6.944\Omega cm$	D' C'
Q13.	A classical gas of molecules each of mass $m$ , is in thermal equilibrium at the absolute temperature	re, T. The
C. L.	velocity components of the molecules along the Cartesian axes are $v_x$ , $v_y$ and $v_z$ . The mean value $\left(v_x\right)$	$+v_{y}$ ) <sup>2</sup> is
	(a) $\frac{k_BT}{m}$ (b) $\frac{3}{2}\frac{k_BT}{m}$ (c) $\frac{1}{2}\frac{k_BT}{m}$ (d) $\frac{2k_BT}{m}$	SOF OPT
Q14.	In a central force field the trajectory of a particle of mass $m$ and angular momentum $L$ in plane polarity of $m$ and $m$ a	ar coordi
TIM	nates is given by $\frac{1}{r} = \frac{m}{L^2} (1 + \varepsilon \cos \theta)$ . Where $\varepsilon$ is the eccentricity of the particle's motion. Which	one of the
E OPTIL	following choices for $\varepsilon$ gives rise to a parabolic trajectory?  (a) $\varepsilon = 0$ (b) $\varepsilon = 1$ (c) $0 < \varepsilon < 1$ (d) $\varepsilon > 1$	.05
CHE OF	(a) $\varepsilon = 0$ (b) $\varepsilon = 1$ (c) $0 < \varepsilon < 1$ (d) $\varepsilon > 1$	ASSI
Q15.	Identify the CORRECT energy band diagram for silicon doped with Arsenic. Here CB, VB, E conduction band, valence band, impurity level and Fermi level, respectively.	<sub>D</sub> and E <sub>F</sub>
ES		CLA
LASSES	(a) $E_{\rm p}$ (b) $E_{\rm p}$ (c) $E_{\rm p}$ (d) $E_{\rm p}$	PIMISI
ST CLI		JE OPTI
Q16.	The first stokes line of a rotational Raman spectrum is observed at 12.96 cm <sup>-1</sup> . Considering the rigi	drotor
OPTIMIS	approximation, the rotational constant is given by (a) $6.48 cm^{-1}$ (b) $3.24 cm^{-1}$ (c) $2.16 cm^{-1}$ (d) $1.62 cm^{-1}$	5
Ox	(a) 5.27cm (b) 5.27cm (c) 2.49cm (d) 1.02cm	T)

Q17. The total energy E of an ideal non-relativistic Fermi gas in three dimensions is given by  $E \propto \frac{N^{3}}{V^{2/3}}$  where N is the number of particles and V is the volume of the gas, Identify the CORRECT equation state (P being the

(a) 
$$PV = \frac{1}{3}E$$

(b) 
$$PV = \frac{2}{3}E$$
 (c)  $PV = E$ 

(c) 
$$PV = E$$

(d) 
$$PV = \frac{5}{3}E$$

Consider the wavefunction  $\psi(\vec{r}_1\vec{r}_2)\chi_s$ , for a fermionic system consisting of two spin-half particles. The spatial part of the wavefunction is given by  $\Psi(\vec{r}_1, \vec{r}_2) = \frac{1}{\sqrt{2}} \left[ \phi_1(\vec{r}_1) \phi_2(\vec{r}_2) + \phi_2(\vec{r}_1) \phi_1(\vec{r}_2) \right]$  where  $\phi_1$  and  $\phi_2$ are single particle state. The spin part  $\chi_s$  of the wavefunction with spin states  $\alpha\left(+\frac{1}{2}\right)$  and  $\beta\left(=\frac{1}{2}\right)$  should be THE (d) BB MIST

(a) 
$$\frac{1}{\sqrt{2}}(\alpha\beta + \beta\alpha)$$
 (b)  $\frac{1}{\sqrt{2}}(\alpha\beta - \beta\alpha)$ 

(b) 
$$\frac{1}{\sqrt{2}}(\alpha\beta - \beta\alpha)$$

(a)  $\frac{1}{\sqrt{2}}(\alpha\beta + \beta\alpha)$  (b)  $\frac{1}{\sqrt{2}}(\alpha\beta - \beta\alpha)$  (c)  $\alpha\alpha$  (d)  $\beta\beta$ The electric and magnetic fields  $\vec{E}(z,t)$  and  $\vec{B}(z,t)$ , respectively corresponding to the scalar potential  $\phi(z,t) = 0$  and vector potential  $\vec{A}(z,t) = \hat{i}tz$  are

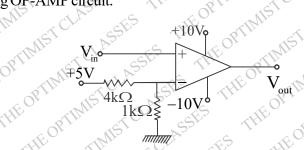
(a) 
$$\vec{E} = \hat{i}z$$
 and  $\vec{B} = -it$ 

(b) 
$$\vec{E} = \hat{i}z$$
 and  $\vec{B} = jt$ 

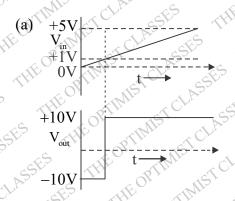
(c) 
$$\vec{E} = -\hat{i}z$$
 and  $\vec{B} = -\hat{j}t$ 

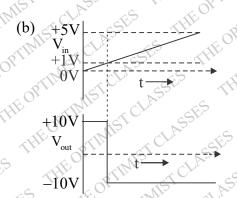
(d) 
$$\vec{E} = -\hat{i}z$$
 and  $\vec{B} = \hat{j}t$ 

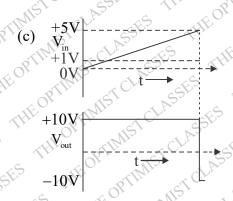
Consider the following OP-AMP circuit

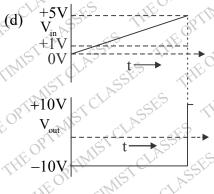


Which one of the following correctly represents the output  $V_{\it out}$  corresponding to the input





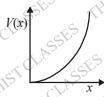




- Q21. Deuteron has only one bound state with spin parity 1<sup>+</sup>, isospin 0 and electric quadrupole moment 0.286 efm These data suggest that the nuclear forces are having
  - (a) Only spin and isospin dependence
- (b) no spin dependence and no tensor components
- (c) spin dependence but no tensor components (d) spin dependence along with tensor components
- A particle of unit mass moves along the x-axis under the influence of a potential,  $V(x) = x(x-2)^2$ . The particle is found to be in stable equilibrium at the point x = 2. The time period of oscillation of the particle is

- Which one of the following CANNOT be explained by considering a harmonic approximation for the lattice vibrations in solids?
  - (a) Debye's  $T^3$  law

- (b) Dulong Petis's law
- (c) Optical branches in lattices
- (d) Thermal expansion
- A particle is constrained to move in a truncated harmonic potential well (x > 0) as shown in the figure. Which one of the following statements is CORRECT:



- (a) The parity of the first excited state is even
  - (b) The parity of the ground state is even
- (c) The ground state energy is  $\frac{1}{2}\hbar\omega$
- (d) Thermal expansion
- The number of independent components of the symmetric tensor  $A_{ij}$  with indices i,j=1,2,3 is
  - (a) 1

Q.26 - Q.55 : Carry TWO marks each.

Consider a system in the unperturbed state described by the Hamiltonian,  $H_0 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ . The system is sub-

jected to a pertubation of the form  $H = \begin{pmatrix} \delta & \delta \\ \delta & \delta \end{pmatrix}$ , where  $\delta << 1$ . The energy eigenvalues of the perturbed

system using the first order pertubation approximation are

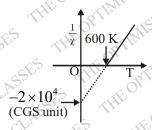
(a) 1 and  $(1+2\delta)$ 

(c)  $(1+2\delta)$  and  $(1-2\delta)$ 

(b)  $(1+\delta)$  and  $(1-\delta)$  Primite (d)  $(1-\delta)$ (d)  $(1+\delta)$  and  $(1-2\delta)$ 

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and the constant, C and C are at time t=0 is given by the constant C and C are at time t=0 is given by the constant C and C are at time t=0 is given by the constant C and C are at time t=0 is given by the constant C and C are at time t=0 is given by the constant C and C are at time t=0 is given by the constant C and C are at time t=0 is given by the constant C and C are at time t=0 is given by the constant C and C are at time t=0 in C. Inverse susceptibility  $(1/\chi)$  as a function of temperature, T for a material undergoing paramagnetic to ferro-Weiss molecular field constant,  $\lambda$ , in CGS units, are magnetic transition is given, in the figure, where O is the origin. The values of the Curie constant, C and the



(a) 
$$C = 5 \times 10^{-5}$$
,  $\lambda = 3 \times 10^{-2}$ 

(b) 
$$C = 3 \times 10^{-2}$$
,  $\lambda = 5 \times 10^{-5}$ 

(c) 
$$C = 3 \times 10^{-2}$$
,  $\lambda = 2 \times 10^{-4}$ 

(d) 
$$C = 2 \times 10^4$$
,  $\lambda = 3 \times 10^{-2}$ 

(d)  $C = 3 \times 10^{-2}$ ,  $\lambda = 5 \times 10^{-5}$ (a)  $C = 2 \times 10^4$ ,  $\lambda = 3 \times 10^{-2}$ (b)  $\lambda = 0$  is given 1 JASSES THE OPTIMIST CLASSES (c)  $C = 3 \times 10^{-5}$ ,  $\lambda = 3 \times 10^{-2}$  (d)  $C = 3 \times 10^{-2}$  (e)  $C = 3 \times 10^{-2}$  (f) (a)  $C = 5 \times 10^{-5}$ ,  $\lambda = 3 \times 10^{-2}$  (b)  $C = 3 \times 10^{-2}$ ,  $\lambda = 5 \times 10^{-5}$  (c)  $C = 3 \times 10^{-2}$ ,  $\lambda = 2 \times 10^{-4}$  (d)  $C = 2 \times 10^{4}$ ,  $\lambda = 3 \times 10^{-2}$  Q28. A plane polarized electromagnetic wave in free space at time t = 0 is given by  $\vec{E}(x, z) = 10\hat{j} \exp\left[i(6x + 8z)\right]$ . The magnetic field  $\vec{B}(x, z, t)$  is given by

(a)  $\vec{B}(x, z, t) = \frac{1}{c}(6\hat{k} - 8\hat{i}) \exp\left[i(6x + 8z - 10ct)\right]$  (b)  $\vec{B}(x, z, t) = \frac{1}{c}(6\hat{k} + 8\hat{i}) \exp\left[i(6x + 8z - 10ct)\right]$  (c)  $\vec{B}(x, z, t) = \frac{1}{c}(6\hat{k} - 8\hat{i}) \exp\left[i(6x + 8z - ct)\right]$  (d)  $\vec{B}(x, z, t) = \frac{1}{c}(6\hat{k} + 8\hat{i}) \exp\left[i(6x + 8z + ct)\right]$ Q29. The eigenvalues of the matrix  $\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$  are

(a) 0, 1, 1 (b)  $0, -\sqrt{2}, \sqrt{2}$  (c)  $\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0$  (d)  $\sqrt{2}, \sqrt{2}, 0$ Q30. Match the typical spectroscopic regions specifical to x = 1 and x = 1.

(a) 
$$\vec{B}(x, z, t) = \frac{1}{c} (6\hat{k} - 8\hat{i}) \exp[i(6x + 8z - 10ct)]$$
 (b)  $\vec{B}(x, z, t) = \frac{1}{c} (6\hat{k} + 8\hat{i}) \exp[i(6x + 8z - 10ct)]$ 

(a) 
$$B(x,z,t) = \frac{1}{c}(6k-8i) \exp[i(6x+8z-ct)]$$
 (b)  $B(x,z,t) = \frac{1}{c}(6k+8i) \exp[i(6x+8z+ct)]$   
(c)  $B(x,z,t) = \frac{1}{c}(6k-8i) \exp[i(6x+8z-ct)]$  (d)  $B(x,z,t) = \frac{1}{c}(6k+8i) \exp[i(6x+8z+ct)]$   
The eigenvalues of the matrix  $\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$  are (a)  $0,1,1$  (b)  $0,-\sqrt{2},\sqrt{2}$  (c)  $\frac{1}{\sqrt{2}},\frac{1}{\sqrt{2}},0$  (d)  $\sqrt{2},\sqrt{2},0$   
Match the typical spectroscopic regions specified in List-I with the corresponding type of transitions in List II and find the correct answer using the codes given below the list:  
List-II

 $(d) \sqrt{2}, \sqrt{2}, 0$  ing type A = 0Q30. Mailed Q30. Mailed Q30. Match the typical spectroscopic regions specified in List -I with the corresponding type of transitions in List -II and find the correct answer using the codes given below the list:

List -I II and find the correct answer using the codes given below the list:

List - I

P. Infrared region Lectronic transitions involving valen
2. Nuclear transitions
3. Vibrational transitions of molecules
4. Transitions involving inner shell electronic transitions
3. Vibrational transitions of molecules
4. Transitions involving inner shell electronic transitions
3. Vibrational transitions of molecules
4. Transitions involving inner shell electronic transitions
3. Vibrational transitions of molecules
4. Transitions involving inner shell electronic transitions
3. Vibrational transitions of molecules
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4. Transitions involving inner shell electronic transitions involving in transitions in transitions involving in transition involving in transition involving in transition involving involving

Q. Ultraviolet visible region

R. X-ray region

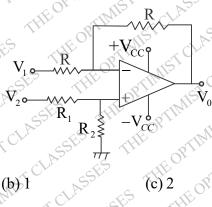
S.  $\gamma$  -rays region

Q31. In the following circuit, for the output voltage to  $V_0 = (-V_1 + V_2/2)$  the ratio  $R_1/R_2$  is  $\frac{233}{CALL} = \frac{233}{CALL} = \frac{233$ A 2 CLASS A 1 PRIMITA

- 1. Electronic transitions involving valence electrons

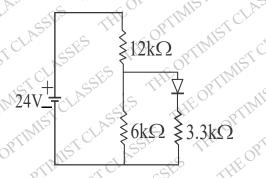
- 4. Transitions involving inner shell electrons.

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- Q32. The terms  $\{\hat{J}_1, \hat{J}_2\}$  arising from  $2s^13d^1$  electronic configuration in J-J scheme are

- In the following circuit, the voltage drop across the ideal diode in forward bias condition is 0.7V



The current passing through the diode is

- (a)  $0.5 \, mA$
- (b) 1.0 mA
- (c) 1.5 mA

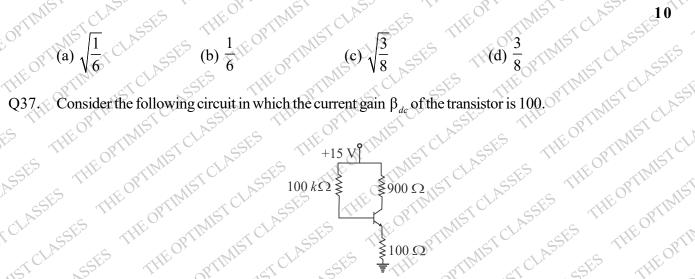
- Chosse the CORRECT statement from the following
  - (a) Neutron interacts through electromagnetic interaction
  - (b) Electron does not interact through weak interaction

  - (d) Quark interacts through strong interaction but not through weak interaction
- A rod of proper length  $\ell_0$  oriented parallel to the x-axis moves with speed 2c/3 along the x-axis in the Sframe, where c is the speed of the light in free space. The observer is also moving along the x-axis with speed c/2 with respect to the S-frame. The length of the rod as measured by the observer is
  - (a)  $0.35 \ell_0$
- (b)  $0.48 \ell_0$

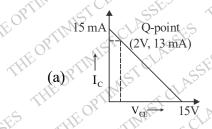
- A simple cubic crystal with lattice parameter  $a_c$  undergoes transition into a tetragonal structure with lattice parameter  $a_t = b_t = \sqrt{2}a_c$  and  $c_t = 2a_c$ , below a certain temperature, the ratio of the interplanar spacings of (101) planes for the cubic and the tetragonal structure is

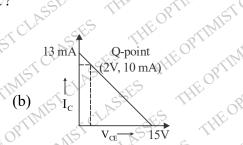
(a) 
$$\sqrt{\frac{1}{6}}$$

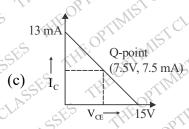
(c) 
$$\sqrt{\frac{3}{8}}$$

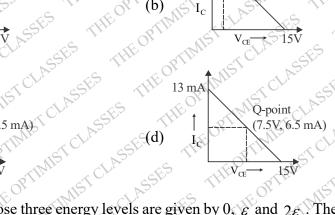


Which one of the following correctly represents the load line (collector current  $I_C$  with respect to collector emitter voltage  $V_{CE}$ ) and Q-point of this circuit? emitter voltage  $V_{CF}$ ) and Q-point of this circuit?









Q38. Consider a system whose three energy levels are given by 0,  $\varepsilon$  and  $2\varepsilon$ . The energy  $\varepsilon$  level is two-fold degenerate and the other two are non-degenerate.  $\beta = \frac{1}{k_B T}$  is given

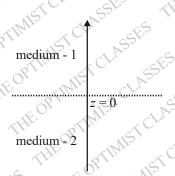
(a) 
$$1 + 2e^{-\beta \epsilon}$$

(b) 
$$2e^{-\beta \epsilon} + e^{-2\beta \epsilon}$$

$$(c)\left(1+e^{-\beta\epsilon}\right)^2$$

(d) 
$$1 + e^{-\beta \in} + e^{-2\beta}$$

Two infinitely extended homogeneous isotropic dielectric media (medium - 1 and medium - 2 with dielectric constants  $\frac{\epsilon_1}{\epsilon_0} = 2$  and  $\frac{\epsilon_2}{\epsilon_0} = 5$ , respectively) meet at the z = 0 planes as shown in the figure. A uniform electric field exists everywhere. For  $z \ge 0$ , the electric field is given by  $\vec{E}_1 = 2\hat{i} - 3\hat{j} + 5\hat{k}$ . The interface separating the two media is charge free. The electric displacement vector in the medium-2 is given by



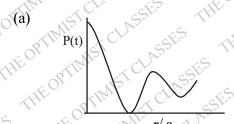
(a) 
$$\vec{D}_2 = \varepsilon_0 \left[ 10\hat{i} + 15\hat{j} + 10\hat{k} \right]$$

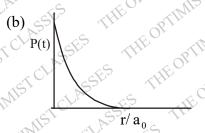
(b) 
$$\vec{D}_2 = \varepsilon_0 \left[ 10\hat{i} - 15\hat{j} + 10\hat{k} \right]$$

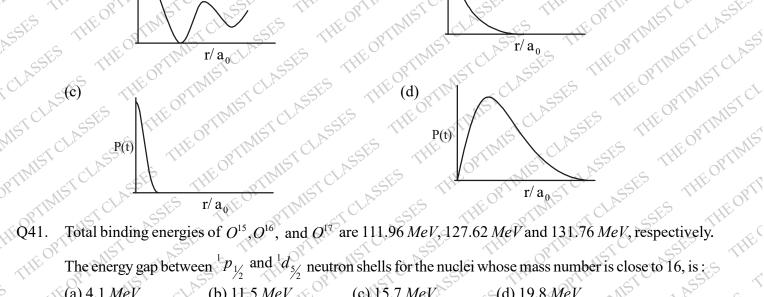
(c) 
$$\vec{D}_2 = \varepsilon_0 \left[ 4\hat{i} - 6\hat{j} + 10\hat{k} \right]$$

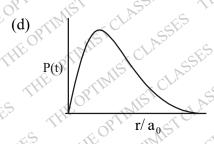
(d) 
$$\vec{D}_2 = \varepsilon_0 \left[ 4\hat{i} + 6\hat{j} + 10\hat{k} \right]$$

 $(b) \ \vec{D}_2 = \vec{\varepsilon}_0 \left[ 10\hat{i} - 15\hat{j} + 10\hat{k} \right]$   $(b) \ \vec{D}_2 = \vec{\varepsilon}_0 \left[ 10\hat{i} - 15\hat{j} + 10\hat{k} \right]$   $(c) \ The ground state wavefunction for the hydrogen atom is given by <math>\Psi_{100} = \frac{1}{\sqrt{4\pi}} \left[ \frac{1}{a_0} \right]^{3/2} e^{-i\hat{r}\hat{r}\hat{r}}$ , where  $a_0$  is the Bohr radius. The plot of the radial probability density, P(r) for the hydrogen atom in the ground state is  $(a) \ P(t) \ T' = a_0$   $(b) \ P(t) \ T' = a_0$   $(c) \ P(t) \ T' = a_0$   $(d) \ The ground state wavefunction for the hydrogen atom in the ground state is
<math display="block">(a) \ P(t) \ T' = a_0$   $(b) \ P(t) \ T' = a_0$   $(c) \ T' = a_0$   $(d) \ T' = a_0$   $(d) \ T' = a_0$   $(e) \ T' = a_0$   $(f) \$ medium- $(a) \ \vec{D}_2 = \varepsilon_0 \Big[ 10\hat{i} + 15\hat{j} + 10\hat{k} \Big]$   $(c) \ \vec{D}_2 = \varepsilon_0 \Big[ 4\hat{i} - 6\hat{j} + 10\hat{r}^{-3} \Big]$   $Q40. \quad \text{The grov}$  $\mathcal{D}_2 = \varepsilon_0 \left[ 10\hat{i} + 15\hat{j} + 10\hat{k} \right]$ (c)  $\vec{D}_2 = \varepsilon_0 \left[ 4\hat{i} - 6\hat{j} + 10\hat{k} \right]$ Q40. The ground state we have

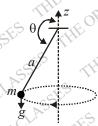








- (a) 4.1 MeV Q42. A= A particle of mass m is attached to a fixed point 'O' by a weightless inextensible string of length a. It is rotating under the gravity as shown in the figure. The Lagrangian of the particle is

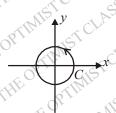


$$L(\theta,\phi) = \frac{1}{2}ma^{2}(\dot{\theta}^{2} + \sin^{2}\theta\dot{\phi}^{2}) - mga\cos\theta$$

Where  $\theta$  and  $\phi$  are the polar angles. The Hamiltonian of the particle is :

- $= \frac{1}{2ma^2} \left( p_{\theta}^2 + \frac{p_{\phi}^2}{\sin^2 \theta} \right) mga \cos \theta \qquad \text{(b) } H = \frac{1}{2ma^2} \left( p_{\theta}^2 + \frac{p_{\phi}^2}{\sin^2 \theta} \right) + mga \cos \theta$

- Given  $\vec{F} = \vec{r} \times \vec{B}$ , where  $\vec{B} = B_0 \left( \hat{i} + \hat{j} + \hat{k} \right)$  is a constant vector and  $\vec{r}$  is the position vector. The value of  $\oint \vec{F} . d\vec{r}$  , where C is a circle of unit radius centered at origin is



- The value of the integral  $\oint_c e^{1/z} dz$ , using the contour C of circle with unit radius |z| = 1, is

- (b)  $1 2\pi i$
- (c)  $1 + 2\pi i$
- A paramagnetic system consisting of N spin-half particles, is placed in an external magnetic field. It is found that N/2 spins are aligned parallel and the remaining N/2 spins are aligned antiparallel to the magnetic field. The statistical entropy of the system is,
- (b)  $\frac{N}{2}k_B \ln 2$  (c)  $\frac{3N}{2}k_B \ln 2$  (d)  $Nk_B \ln 2$
- Q46. The equilibrium vibration frequency for a oscillator is observed at  $2990 \, cm^{-1}$ . The ratio of the frequencies corresponding to the first and the fundamental spacetral lines is 1.96. Considering the oscillator to be anharmonic, the anharmonicity constant is
  - (a) 0.005
- (b) 0.02

- At a certain temperature T, the average speed of nitrogen molecules in air is found to be 400m/s. The most probable and the root mean square speeds of the molecules are, respectively,
  - (a)  $355 \, m/s$ ,  $434 \, m/s$

(b) 820 m/s, 917 m/s

(c) 152 m/s, 301 m/s

(d)  $422 \, m/s$ ,  $600 \, m/s$ 

Common Data for Questions 48 and 49.

The wavefunction of a particle moving in free space is given by  $\Psi$ 

- The energy of the particle is
- (b)  $\frac{3\hbar^2 k^2}{4m}$
- (c)  $\frac{\hbar^2 k^2}{2m}$
- The probability current density for the real part of the wavefunction is

  (a) 1

  (b)  $\frac{\hbar^2 k}{m}$ (a) 1

  (b)  $\frac{\hbar k}{m}$

### Common Data for Questions 50 and 51.

The dispersion relation for a one dimensional monatomic crystal with lattice spacing a, which interacts via nearest neighbour harmonic potential is given by  $\omega = A \left| \sin \frac{Ka}{2} \right|$ , where A is a constant of a appropriate unit.

The group velocity at the boundary of the first Brillouin zone is

Q51. The force constant between the nearest neighour of the lattice is (M is the mass of the atom)

## Statement for Linked Answer Q.52 and Q.53

In a hydrogen atom, consider that the electronic charge is uniformly distributed in a spherical volume of radius  $a = 0.5 \times 10^{-10} \, m$  around the proton. The atom is paleed in a uniform electric field  $E = 30 \times 10^5 \, V \, / \, m$ . Assume that the order  $= 30 \times 10^5 \, V \, / \, m$ . sume that the spherical distribution of the negative charge remains undistorted under the electric field

In the equilibrium condition, the separation between the positive and the negative charge centers is

(a)  $8.66 \times 10^{-16} m$ 

(b)  $2.60 \times 10^{-15} m$ 

(c)  $2.60 \times 10^{-16} m$ 

(d)  $8.66 \times 10^{-1}$ 

The polarizability of the hydrogen atom in unit of  $(C^2m/N)$  is

(a)  $2.0 \times 10^{-40}$ 

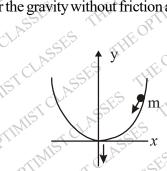
(b)  $1.4 \times 10^{-41}$ 

(c)  $1.4 \times 10^{-40}$ 

(d)  $2.0 \times 10^{-1}$ 

### Statement for Linked Answer Q.54 and Q.55

A particle of mass m slides under the gravity without friction along parabolic path  $y = ax^2$  as shown in the figure Here a is a constant.



The Lagrangian for this particle is given by,

(a)  $L = \frac{1}{2} m \dot{x}^2$ 

ven by,  $L = \frac{1}{2}m(1+4a^2x^2)$ 

(c)  $L = \frac{1}{2}m\dot{x}^2 + mgax^2$ 

(d)  $L = \frac{1}{2}m(1+4a^2x^2)\dot{x}^2 + mgax^2$ 

The Lagrange's equation of motion of the particle is

(a)  $\ddot{x} = 2gax$ 

 $-4ma^2x\dot{x}^2$ (b)  $m(1+4a^2x^2)\ddot{x} = -2mgax$ 

(c)  $m(1+4a^2x^2)\ddot{x} = 2mgax + 4ma^2x\dot{x}^2$ 

(d)  $\ddot{x} = -2gax$ 

## ANSWER KEY

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