

THE OPTIMIST CLASSES IIT-JAM TOPPERS



MANOJ KUMAR SINGH



ABHAY



PAWAN



SATYAM



SOUMIL GIRISH SAHU



BHOOMIJA



AKSHIT AGGARWAL



SHIKHAR CHAMOLI



RAVI SINGH ADHIKARI



GAURAV JHA



SWAPNIL JOSHI



LOKESH BHATT



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VAIBHAV

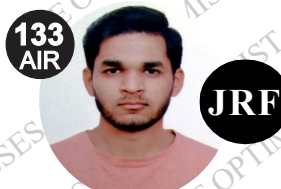


SHASWAT CHAMOLI

CSIR-NET-JRF RESULTS 2022



ANNU
DL01000308



ALANKAR
UP15000162



SAHIL RANA
HR09000108



JAYESTHI
RJ11000161



DASRATH
RJ06000682



VIVEK
UK01000439



UZAIR AHMED
UP02000246



SURYA PRATAP SINGH
RJ06000232



HIMANSHU
UP10000095



CHANDAN
RJ09000159



SAIKHOM JOHNSON
MN01000196



AJAY SAINI
RJ06001744



VIKAS YADAV
RJ06001102



JYOTSNA KOHLI
UK02000262



SHYAM SUNDAR
RJ06000615

THE OPTIMIST CLASSES

AN INSTITUTE FOR NET-JRF/GATE/IIT-JAM/JEST/TIFR/M.Sc ENTRANCE EXAMS

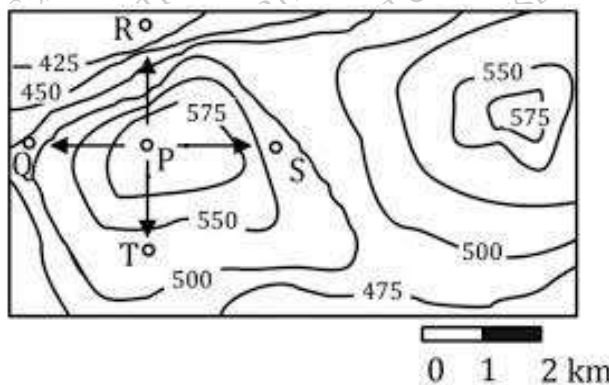
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GATE PAPER 2017

SECTION - A

- Q1. The ninth and the tenth of this month are Monday and Tuesday _____.
- (a) figuratively (b) retrospectively (c) respectively (d) rightfully
- Q2. It is _____ to read this year's textbook _____ the last year's.
- (a) easier, than (b) most easy, than (c) easier, from (d) easiest, from
- Q3. A rule states that in order to drink beer, one must be over 18 years old. In a bar, there are 4 people, P is 16 years old, Q is 25 years old, R is drinking milkshake and S is drinking a beer. What must be checked to ensure that the rule is being followed?
- (a) Only P 's drink (b) Only P 's drink and S 's age
(c) Only S 's age (d) Only P 's drink, Q 's drink and S 's age
- Q4. Fatima starts from point P , goes North for 3km , and then East for 4km to reach point. She then turns to face point P and goes 15km in that direction. She then goes North for 6km . How far is she from point P , and in which direction should she go to reach point P ?
- (a) 8km , East (b) 12km , North (c) 6km , East (d) 10km , North
- Q5. 500 students are taking one or more courses out of Chemistry, Physics and Mathematics. Registration records indicate course enrolment as follows: Chemistry (329), Physics (186), Mathematics (295), Chemistry and Physics (83), Chemistry and Mathematics (217), and Physics and Mathematics (63). How many students are taking all 3 subjects?
- (a) 37 (b) 43 (c) 47 (d) 53
- Q6. "If you are looking for a history of India, or for an account of the rise and fall of the British Raj, or for the reason of the cleaving of the subcontinent into two mutually antagonistic parts and the effects this mutilation will have in the respective sections, and ultimately on Asia, you will not find it in these pages: for though I have spent a lifetime in the country, I lived too near the seat of events, and was too intimately associated with the actors, to get the perspective needed for the impartial recording of these matters."
Which of the following statements best reflects the author's opinion?
- (a) An intimate association does not allow for the necessary perspective.
(b) Matters are recorded with an impartial perspective.
(c) An intimate association offers an impartial perspective.
(d) Actors are typically associated with the impartial recording of matters.
- Q7. Each of P, Q, R, S, W, X, Y and Z has been married at most once, X and Y are married and have two children P and Q, Z is the grandfather of the daughter S of P . Further, Z and W are married and are parents of R . Which one of the following must necessarily be FALSE?
- (a) X is the mother-in-law of R (b) P and R not married to each other
(c) P is a son of X and Y (d) Q cannot be married to R
- Q8. 1200 men and 500 women can build a bridge in 2 weeks. 900 men and 250 women will take 3 weeks to build the same bridge. How many men will be needed to build the bridge in one week?
- (a) 3000 (b) 3300 (c) 3600 (d) 3900

- Q9. The number of 3-digit numbers such that the digit 1 is never to the immediate right of 2 is
 (a) 781 (b) 791 (c) 881 (d) 891
- Q10. A contour line joins locations having the same height above the mean sea level. The following is a contour plot of a geographical region. Contour lines are shown at 25m intervals in this plot.



Which of the following is the steepest path leaving from P?

- (a) P to Q (b) P to R (c) P to S (d) P to T

SECTION - B

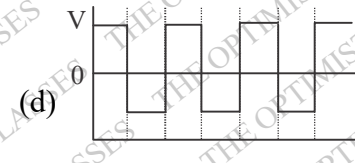
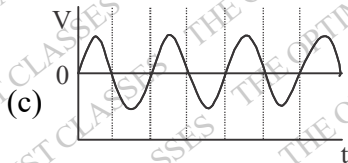
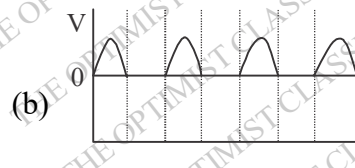
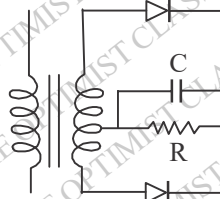
Q.1 - Q.25 : Carry ONE mark each.

- Q1. In the nuclear reaction $^{13}\text{C}_6 + \nu_e \rightarrow ^{13}\text{N}_7 + X$, the particle X is
 (a) an electron (b) an anti-electron (c) a muon (d) a pion
- Q2. Two identical masses of 10gm each are connected by a massless spring of spring constant 1N/m. The non-zero angular eigen frequency of the system is _____ rad/s. (upto two decimal places).
- Q3. Consider a triatomic molecule of the shape shown in the figure below in three dimensions. The heat capacity of this molecule at high temperature (temperature much higher than the vibrational and rotational energy scales of the molecule but lower than its bond dissociation energies is:



- (a) $\frac{3}{2}k_B$ (b) $3k_B$ (c) $\frac{9}{2}k_B$ (d) $6k_B$
- Q4. For the Hamiltonian $H = a_0 I + \vec{b} \cdot \vec{\sigma}$ where $a_0 \in \mathbb{R}$, \vec{b} is a real vector, I is the 2×2 identity matrix and $\vec{\sigma}$ are the Pauli matrices, the ground state energy is
 (a) $|b|$ (b) $2a_0 - |b|$ (c) $a_0 - |b|$ (d) a_0
- Q5. The Poisson bracket $[x, xp_y + yp_x]$ is equal to
 (a) $-x$ (b) y (c) $2p_x$ (d) p_y
- Q6. The wavefunction of which orbital is spherically symmetric:
 (a) p_x (b) p_y (c) s (d) d_{xy}
- Q7. A monochromatic plane wave in free space with electric field amplitude of 1V/m is normally incident on a fully reflecting mirror. The pressure exerted on the mirror is _____ $\times 10^{-12}$ Pa. (Up to two decimal places)

- Q8. The electronic ground state energy of the Hydrogen atom is -13.6 eV . The highest possible electronic energy eigenstate has an energy equal to
 (a) 0 (b) 1 eV (c) $+13.6 \text{ eV}$ (d) ∞
- Q9. Consider a one-dimensional lattice with a weak periodic potential $U(x) = U_0 \cos\left(\frac{2\pi x}{a}\right)$. The gap at the edge of the Brillouin zone $\left(k = \frac{\pi}{a}\right)$ is:
 (a) U_0 (b) $\frac{U_0}{2}$ (c) $2U_0$ (d) $\frac{U_0}{4}$
- Q10. Identical charge q are placed at five vertices of a regular hexagon of side a . The magnitude of the electric field and the electrostatic potential at the centre of the hexagon are respectively
 (a) 0, 0 (b) $\frac{q}{4\pi\epsilon_0 a^2}, \frac{q}{4\pi\epsilon_0 a}$ (c) $\frac{q}{4\pi\epsilon_0 a^2}, \frac{5q}{4\pi\epsilon_0 a}$ (d) $\frac{\sqrt{5}q}{4\pi\epsilon_0 a^2}, \frac{\sqrt{5}q}{4\pi\epsilon_0 a}$
- Q11. A reversible Carnot engine is operated between temperatures T_1 and T_2 ($T_2 > T_1$) with a photon gas as the working substance. The efficiency of the engine is
 (a) $1 - \frac{3T_1}{4T_2}$ (b) $1 - \frac{T_1}{T_2}$ (c) $1 - \left(\frac{T_1}{T_2}\right)^{3/4}$ (d) $1 - \left(\frac{T_1}{T_2}\right)^{4/3}$
- Q12. The best resolution that a 7 bit A/D converter with 5 V full scale can achieve is _____ mV .
 (Up to two decimal places).
- Q13. If the Lagrangian $L_0 = \frac{1}{2} m \left(\frac{dq}{dt}\right)^2 - \frac{1}{2} m \omega^2 q^2$ is modified to $L = L_0 + \alpha q \left(\frac{dq}{dt}\right)$, which one of the following is TRUE?
 (a) Both the canonical momentum and equation of motion do not change
 (b) Canonical momentum changes, equation of motion does not change
 (c) Canonical momentum does not change, equation of motion changes
 (d) Both the canonical momentum and equation of motion change
- Q14. A parallel plate capacitor with square plates of side 1 m separated by 1 micro meter is filled with a medium of dielectric constant of 10. If the charges on the two plates are 1 C and -1 C , the voltage across the capacitor is _____ kV . (up to two decimal places). ($\epsilon_0 = 8.854 \times 10^{-12} \text{ F / m}$)
- Q15. The contour integral $\oint \frac{dz}{1+z^2}$ evaluated along a contour going from $-\infty$ to $+\infty$ along the real axis and closed in the lower half-plane by a half circle is equal to _____. (Up to two decimal places).
- Q16. In the figure given below, the input to the primary of the transformer is a voltage varying sinusoidally with time. The resistor R is connected to the centre tap of the secondary. Which one of the following plots represents the voltage across the resistor R as a function of time?



Q17. Light is incident from a medium of refractive index $n = 1.5$ onto vacuum. The smallest angle of incidence for which the light is not transmitted into vacuum is _____ degrees. (Upto two decimal places).

Q18. Electromagnetic interactions are :

- (a) C conserving (b) C non-conserving but CP conserving
(c) CP non-conserving but CPT conserving (d) CPT non-conserving

Q19. The Compton wavelength of a proton is _____ fm . (up to two decimal places).

$$(m_p = 1.67 \times 10^{-27} \text{ kg}, h = 6.626 \times 10^{-34} \text{ Js}, e = 1.602 \times 10^{-19} \text{ C}) :$$

Q20. Which one of the following conservation laws is violated in the decay $\tau^+ \rightarrow \mu^+ \mu^+ \mu^-$

- (a) Angular momentum (b) Total Lepton number
(c) Electric charge (d) Tau number

Q21. The coefficient of e^{ikx} in the Fourier expansion of $u(x) = A \sin^2(ax)$ for $k = -2a$ is

- (a) $A/4$ (b) $-A/4$ (c) $A/2$ (d) $-A/2$

Q22. The phase space trajectory of a free particle bouncing between two hard walls elastically in one dimension is a

- (a) straight line (b) parabola (c) rectangle (d) circle

Q23. The atomic mass and mass density of sodium are 23 and 0.968 g cm^{-3} , respectively. The number density of valence electrons is _____ $\times 10^{22} \text{ cm}^{-3}$. (Upto two decimal places.)

$$(\text{Avogadro number, } N_A = 6.022 \times 10^{23}).$$

Q24. The degeneracy of the third energy level of a 3-dimensional isotropic quantum harmonic oscillator is

- (a) 6 (b) 12 (c) 8 (d) 10

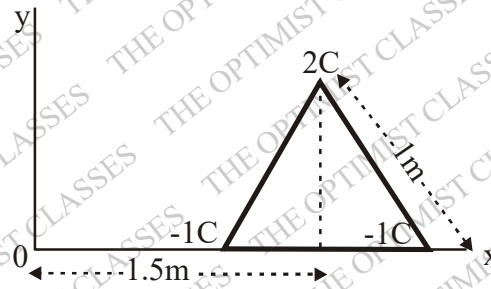
Q25. A one dimensional simple harmonic oscillator with Hamiltonian $H_0 = \frac{p^2}{2m} + \frac{1}{2}kx^2$ is subjected to a small perturbation, $H_1 = \alpha x + \beta x^3 + \gamma x^4$. The first order correction to the ground state energy is dependent on

- (a) only β (b) α and γ (c) α and β (d) only γ

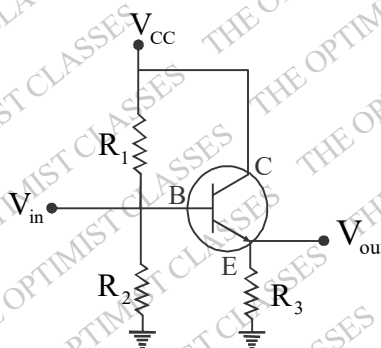
Q.26 - Q.55 : Carry TWO marks each.

Q26. Three charges ($2C, -1C, -1C$) are placed at the vertices of an equilateral triangle of side $1m$ as shown in the

figure. The component of the electric dipole moment about the marked origin along the y direction is _____ cm.



- Q27. An object travels along the x -direction with velocity $c/2$ in a frame O . An observer in a frame O' sees the same object travelling with velocity $c/4$. The relative velocity of O' with respect to O in units of c is _____ . (up to two decimal places).
- Q28. The energy density and pressure of a photon gas are given by $u = aT^4$ and $P = u/3$, where T is the temperature and a is the radiation constant. The entropy per unit volume is given by αaT^3 . The value of α is _____ (up to two decimal places.)
- Q29. A person weighs w_p at Earth's north pole and w_e at the equator. Treating the Earth as a perfect sphere of radius 6400km , the value $100 \times (w_p - w_e) / w_p$ is _____. (Upto two decimal palces).
(Take $g = 10\text{m/s}^2$)
- Q30. The minimum number of NAND gates required to construct an OR gate is :
(a) 2 (b) 4 (c) 5 (d) 3
- Q31. The total energy of an inert-gas crystal is given by $E(R) = \frac{0.5}{R^{12}} - \frac{1}{R^6}$ (in eV), where R is the inter-atomic spacing in Angstroms. The equilibrium separation between the atoms is _____ Angstroms.
(Upto two decimal places).
- Q32. The imaginary part of an analytic complex function is $v(x, y) = 2xy + 3y$. The real part of the function is zero at the origin. The value of the real part of the function at $1 + i$ is _____. (Upto two decimal places).
- Q33. Consider N non-interacting, distinguishable particles in a two-level system at temperature T . The energies of the levels are 0 and ε , where $\varepsilon > 0$. In the high temperature limit ($k_B T \gg \varepsilon$), what is the population of particles in the level with energy ε ?
(a) $\frac{N}{2}$ (b) N (c) $\frac{N}{4}$ (d) $\frac{3N}{4}$
- Q34. For the transistor amplifier circuit shown below with $R_1 = 10\text{k}\Omega$, $R_2 = 10\text{k}\Omega$, $R_3 = 1\text{k}\Omega$, and $\beta = 99$. Neglecting the emitter diode resistance, the input impedance of the amplifier looking into the base for small A.C. signal is _____ $\text{k}\Omega$. (up to decimal places).



- Q35. Which one of the following gases of diatomic molecules is Raman, infrared, and NMR active?
 (a) $^1\text{H}-^1\text{H}$ (b) $^{12}\text{C}-^{16}\text{O}$ (c) $^1\text{H}-^{35}\text{Cl}$ (d) $^{16}\text{O}-^{16}\text{O}$
- Q36. Let X be a column vector of dimension $n > 1$ with at least one-zero entry. The number of non-zero eigenvalues of the matrix $M = XX^T$ is
 (a) 0 (b) n (c) 1 (d) $n - 1$
- Q37. A free electron of energy $1eV$ is incident upon a one-dimensional finite potential step of height $0.75eV$. The probability of its reflection from the barrier is _____. (Upto two decimal places)
- Q38. An infinite solenoid carries a time varying current $I(t) = At^2$, with $A \neq 0$. The axis of the solenoid is along the \hat{z} direction \hat{r} and $\hat{\theta}$ are the usual radial and polar directions in cylindrical polar coordinates $\vec{B} = B_r\hat{r} + B_\theta\hat{\theta} + B_z\hat{z}$ is the magnetic field at a point outside the solenoid. Which one of the following statements is true?
 (a) $B_r = 0, B_\theta = 0, B_z = 0$ (b) $B_r \neq 0, B_\theta \neq 0, B_z = 0$
 (c) $B_r \neq 0, B_\theta \neq 0, B_z \neq 0$ (d) $B_r = 0, B_\theta = 0, B_z \neq 0$
- Q39. Consider two particles and two non-degenerate quantum levels 1 and 2. Level 1 always contains a particle. Hence, what is the probability that level 2 also contains a particle for each of the two cases:
 (i) when the two particles are distinguishable and
 (ii) when the two particles are bosons?
 (a) (i) 1/2 and (ii) 1/3 (b) 1/2 and (ii) 1/2 (c) (i) 2/3 and 1/2 (d) (i) 1 and (ii) 0
- Q40. The real space primitive lattice vectors are $\vec{a}_1 = a\hat{x}$ and $\vec{a}_2 = \frac{a}{2}(\hat{x} + \sqrt{3}\hat{y})$. The reciprocal space unit vectors \vec{b}_1 and \vec{b}_2 for this lattice are, respectively
 (a) $\frac{2\pi}{a}\left(\hat{x} - \frac{\hat{y}}{\sqrt{3}}\right)$ and $\frac{4\pi}{a\sqrt{3}}\hat{y}$ (b) $\frac{2\pi}{a}\left(\hat{x} + \frac{\hat{y}}{\sqrt{3}}\right)$ and $\frac{4\pi}{a\sqrt{3}}\hat{y}$
 (c) $\frac{2\pi}{a\sqrt{3}}\hat{x}$ and $\frac{4\pi}{a}\left(\frac{\hat{x}}{\sqrt{3}} + \hat{y}\right)$ (d) $\frac{2\pi}{a\sqrt{3}}\hat{x}$ and $\frac{4\pi}{a}\left(\frac{\hat{x}}{\sqrt{3}} - \hat{y}\right)$
- Q41. The geometric cross-section of two colliding protons at large energies is very well estimated by the product of the effective sizes of each particle. This is closest to
 (a) $10 b$ (b) $10 mb$ (c) $10 \mu b$ (d) $10 pb$
- Q42. A uniform volume charge density is placed inside a conductor (with resistivity $10^{-2} \Omega\text{m}$). The charge density becomes 1/(2.718) of its original value after time _____ femto seconds. (Up to two decimal places) ($\epsilon_0 = 8.854 \times 10^{-12} \text{ F/m}$)
- Q43. Water freezes at 0°C at atmospheric pressure ($1.01 \times 10^5 \text{ Pa}$). The densities of water and ice at this temperature and pressure are 1000 kg/m^3 and 934 kg/m^3 respectively. The latent heat of fusion is $3.34 \times 10^5 \text{ J/kg}$. The pressure required for depressing the melting temperature of ice by 10°C is _____ GPa . (Upto two decimal places)
- Q44. The integral $\int_0^\infty x^2 e^{-x^2} dx$ is equal to _____. (Upto two decimal places).
- Q45. J^p for the ground state of the $^{13}\text{C}_6$ nucleus is _____

- (a) 1^+ (b) $\frac{3^-}{2}$ (c) $\frac{3^+}{2}$ (d) $\frac{1^-}{2}$

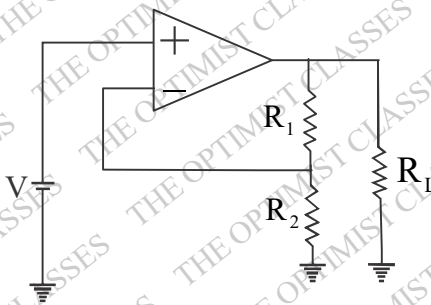
Q46. A uniform solid cylinder is released on a horizontal surface with speed $5m/s$ without any rotation (slipping without rolling). The cylinder eventually starts rolling without slipping. If the mass and radius of the cylinder are $10gm$ and $1cm$ respectively, the final linear velocity of the cylinder is _____ m/s . (Up to two decimal places)

Q47. Consider a one-dimensional potential well of width $3nm$. Using the uncertainty principle ($\Delta x \Delta p \geq \hbar/2$), an estimate of the minimum depth of the well such that it has at least one bound state for an electron is

$$(m_e = 9.31 \times 10^{-31} \text{ kg}, h = 6.626 \times 10^{-34} \text{ Js}, e = 1.602 \times 10^{-19} \text{ C}):$$

- (a) $1\mu eV$ (b) $1meV$ (c) $1eV$ (d) $1MeV$

Q48. Consider an ideal operational amplifier as shown in the figure below with $R_1 = 5k\Omega$, $R_2 = 1k\Omega$, $R_L = 100k\Omega$. For an applied input voltage $V = 10mV$, the current passing through R_2 is _____ μA . (Up to two decimal places).



Q49. The π^+ decays at rest to μ^+ and ν_μ . Assuming the neutrino to be massless, the momentum of the neutrino is _____ MeV/c . (Up to two decimal places). ($m_\pi = 139 \text{ MeV}/c^2$, $m_\mu = 105 \text{ MeV}/c^2$)

Q50. Consider the differential equation $\frac{dy}{dx} + y \tan x = \cos(x)$. If $y(0) = 0$, $y(\pi/3)$ is _____. (Up to two decimal places)

Q51. Consider a metal with free electron density of $6 \times 10^{22} \text{ cm}^{-3}$. The lowest frequency electromagnetic radiation to which this metal is transparent is $1.38 \times 10^{16} \text{ Hz}$. If this metal had a free electron density of $1.8 \times 10^{23} \text{ cm}^{-3}$ instead, the lowest frequency electromagnetic radiation to which it would be transparent is _____ $\times 10^{16} \text{ Hz}$. (up to two decimal places).

Q52. Using Hund's rule, the total angular momentum quantum number J for the electronic ground state of the nitrogen atom is

- (a) $1/2$ (b) $3/2$ (c) 0 (d) 1

Q53. Consider a 2-dimensional electron gas with a density of 10^{19} m^{-2} . The Fermi energy of the system is _____ eV . (Up to two decimal places).

$$(m_e = 9.31 \times 10^{-31} \text{ kg}, h = 6.626 \times 10^{-34} \text{ Js}, e = 1.602 \times 10^{-19} \text{ C})$$

Q54. Which one of the following operators is Hermitian?

(a) $i \frac{(p_x x^2 - x^2 p_x)}{2}$ (b) $i \frac{(p_x x^2 + x^2 p_x)}{2}$ (c) $e^{ip_x a}$ (d) $e^{-ip_x a}$

Q55. Positronium is an atom made of an electron and a positron. Given the Bohr radius for the ground state of the Hydrogen atom to be 0.53 Angstroms, the Bohr radius for the ground state of positronium is _____ Angstroms. (Up to two decimal places.)

ANSWER KEY

SECTION - A

- | | | | |
|--------|---------|--------|--------|
| 1. (c) | 2. (a) | 3. (b) | 4. (a) |
| 5. (d) | 6. (a) | 7. (d) | 8. (c) |
| 9. (c) | 10. (b) | | |

SECTION - B

- | | | | |
|----------------------|----------------------|--------------------|----------------------|
| 1. (a) | 2. (14.10 to 14.20) | 3. (d) | 4. (c) |
| 5. (b) | 6. (c) | 7. (8.80 to 8.90) | 8. (d) |
| 9. (a) | 10. (c) | 11. (b) | 12. (39.30 to 39.50) |
| 13. (b) | 14. (11.25 to 11.34) | 15. (3.13 to 3.15) | 16. (a) |
| 17. (41.60 to 42.00) | 18. (a) | 19. (1.30 to 1.34) | 20. (d) |
| 21. (b) | 22. (c) | 23. (2.50 to 2.55) | 24. (a) |
| 25. (d) | 26. (1.72 to 1.75) | 27. (0.27 to 0.31) | 28. (1.30 to 1.36) |
| 29. (0.32 to 0.36) | 30. (d) | 31. (0.90 to 1.10) | 32. (2.90 to 3.10) |
| 33. (a) | 34. (4.75 to 5.01) | 35. (c) | 36. (c) |
| 37. (0.10 to 0.12) | 38. (d) | 39. (c) | 40. (a) |
| 41. (b) | 42. (87.50 to 89.50) | 43. (0.15 to 0.19) | 44. (0.43 to 0.45) |
| 45. (d) | 46. (3.30 to 3.35) | 47. (b) | 48. (9.80 to 10.20) |
| 49. (29.50 to 30.10) | 50. (0.51 to 0.53) | 51. (2.35 to 2.45) | 52. (b) |
| 53. (2.31 to 2.40) | 54. (a) | 55. (0.99 to 1.10) | |