

# THE OPTIMIST CLASSES IIT-JAM TOPPERS



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# CSIR-NET-JRF RESULTS 2022



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# THE OPTIMIST CLASSES

AN INSTITUTE FOR NET-JRF/GATE/IIT-JAM/JEST/TIFR/M.Sc ENTRANCE EXAMS

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## TATA INSTITUTE OF FUNDAMENTAL RESEARCH (TIFR) PREVIOUS YEAR QUESTIONS YEAR 2010

Name :- ..... Ref. Code :- ..... Date :- .....

**Please read all instructions carefully before you attempt the questions**

1. Please fill-in details about name, reference code etc. on the question paper and answer sheet. Answer sheet is machine-readable. Read the instructions given on the reverse of the answer sheet before you start filling it up. Use only HB pencils to fill-in the answer sheet.
2. Indicate your ANSWER ON THE ANSWER SHEET by blackening the appropriate circle for each questions. *Do not mark more than one circle for any question*: this will be treated as a wrong answer.
3. This test comes in two sections, **Section A** and **Section B**, both of which contain multiple choice-type questions. Only ONE of the options given at the end of each question is correct. Section A contains 20 questions, each with 4 options, and Section B contains 8 questions, each with 6 options. The maximum marks are 60 for section A plus 40 for Section B, totaling to 100. Marking shall be as:
  - (i) If the answer is **correct** : +3 marks in Section A: +5 marks in Section B.
  - (ii) If the answer is **incorrect** : -1 mark in both Section A & B.
  - (iii) If the answer is not **attempted**: 0 marks in both Section A & B.
  - (iv) If more than one box is **marked**: 0 marks in both Section A & B.

Note that negative marking as indicated above will be implemented.
4. As a rough guideline, the time spent on questions in Section A should be about 5 minutes each; questions in Section B should take about 10 minutes each. Obviously, some questions may take a little less time while others may require a little more.
5. We advise you to first mark the correct answer on the Question PAPER and then to TRANSFER these to the ANSWER SHEET only when you are sure of your choice.
6. Rough work may be done on blank pages of the question paper. If needed, you may ask for extra rough sheets from an invigilator.
7. **Use of calculators is permitted.** Calculator which plots graphs is NOT allowed. Multiple-use devices such as cell phones, smart phones etc., CANNOT be used for this purpose.
8. Do NOT ask for clarifications from the invigilators regarding the questions. They have been instructed not to respond any such inquiries from candidates. In case a Correction/clarification is deemed necessary; the invigilator(s) will announce it publicly.

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## SECTION :- A

20 × 3 = 60 Marks

Q.1 The matrix

$$\begin{pmatrix} 1 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix}$$

can be related by a similarity transformation to the matrix

(a)  $\begin{pmatrix} 1 & -1 & 1 \\ 1 & -1 & 1 \\ 1 & 1 & 0 \end{pmatrix}$

(b)  $\begin{pmatrix} 2 & 1 & 0 \\ 1 & -1 & -1 \\ 0 & -1 & 2 \end{pmatrix}$

(c)  $\begin{pmatrix} 1 & -1 & 0 \\ -1 & 1 & 1 \\ 0 & 1 & -1 \end{pmatrix}$

(d)  $\begin{pmatrix} 1 & -1 & 0 \\ -1 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix}$

Q.2 A car tyre is slowly pumped up to a pressure of 2 atmospheres in an environment at 15° C. At this point, it bursts. Assuming the sudden expansion of the air (a mixture of O<sub>2</sub> and N<sub>2</sub>) that was inside the tyre to be adiabatic, its temperature after the burst is

(a) -55° C

(b) -37° C

(c) -26° C

(d) +9° C

Q.3 A small meteor approaches the Earth. When it is at a large distance, it has velocity  $v_\infty$ , and impact parameter  $b$ . If  $R_e$  is the radius of the Earth and  $v_0$  is the escape velocity, the condition for the meteor to strike the Earth is

(a)  $b < R_e \sqrt{1 - (v_0 / v_\infty)^2}$

(b)  $b > R_e \sqrt{1 + (v_0 / v_\infty)^2}$

(c)  $b < R_e \sqrt{1 + (v_0 / v_\infty)^2}$

(d)  $b = R_e (v_0 / v_\infty)$

Q.4 Consider a very, thin wire of uniformly circular cross section. The diameter of the wire is of the order of microns. The correct equipment required to measure the precise value of resistivity of this wire is

(a) ammeter, voltmeter, scale, slide calipers

(b) ammeter, magnet, screw gauge, thermometer

(c) voltmeter, magnet, screw gauge, scale

(d) ammeter, voltmeter, scale, monochromatic laser source

Q.5 A function  $f(x)$  is defined in the range  $-1 \leq x \leq 1$  by

$$f(x) = \begin{cases} 1 - x & \text{for } x \geq 0 \\ 1 + x & \text{for } x < 0 \end{cases}$$

The first few terms in the Fourier series approximating this function are

(a)  $\frac{1}{2} + \frac{4}{\pi^2} \cos \pi x + \frac{4}{9\pi^2} \cos 3\pi x + \dots$

(b)  $\frac{1}{2} + \frac{4}{\pi^2} \sin \pi x + \frac{4}{9\pi^2} \sin 3\pi x + \dots$

(c)  $\frac{4}{\pi^2} \cos \pi x + \frac{4}{9\pi^2} \cos 3\pi x + \dots$

(d)  $\frac{1}{2} - \frac{4}{\pi^2} \cos \pi x + \frac{4}{9\pi^2} \cos 3\pi x - \dots$

Q.6 A lead container contains 1 gm of a  ${}^{60}_{27}\text{Co}$  radioactive source. It is known that a  ${}^{60}_{27}\text{Co}$  nucleus emits a  $\beta$  particle of energy  $316 \text{ KeV}$  followed by two  $\gamma$  emissions of energy  $1173$  and  $1333 \text{ KeV}$  respectively. Which of the following experimental methods would be the best way to determine the lifetime of this  ${}^{60}_{27}\text{Co}$  source?

- (a) Measure the change in temperature of the source  
 (b) Measure the weight of the source now and again after one year  
 (c) Measure the recoil momentum of the nucleus during  $\beta$  emission  
 (d) Measure the number of  $\gamma$  photons emitted by this source

Q.7 A beam of hydrogen molecules travels in the  $z$  direction with a kinetic energy of  $1 \text{ eV}$ . The molecules are in an excited state, from which they decay and dissociate into two hydrogen atoms. When one of the dissociated atoms has its final velocity perpendicular to the  $z$  direction, its kinetic energy is always  $0.8 \text{ eV}$ . The energy released in the dissociative reaction is

- (a)  $0.26 \text{ eV}$                       (b)  $2.6 \text{ eV}$                       (c)  $0.36 \text{ eV}$                       (d)  $3.6 \text{ eV}$

Q.8 Two parallel plates of metal sandwich a dielectric pad of thickness  $d$ , forming an ideal capacitor of capacitance  $C$ . The dielectric pad is elastic, having a spring constant  $k$ . If an ideal battery of voltage  $V$  across its terminals is connected to the two plates of this capacitor, the fractional change  $\delta d / d \ll 1$  in the gap between the plates is

- (a) zero                      (b)  $+\frac{1}{2} \frac{CV^2}{kd^2}$                       (c)  $-\frac{1}{2} \frac{CV^2}{kd^2 + CV^2}$                       (d)  $-\frac{1}{2} \frac{CV^2}{kd^2 - CV^2}$

Q.9 When white light is scattered from a liquid, a strong absorption line is seen at  $400 \text{ nm}$ , and two emission lines are observed, one of which is at  $500 \text{ nm}$ , and another in the infrared portion of the spectrum. The wavelength of this second emission line is

- (a)  $900 \text{ nm}$                       (b)  $2000 \text{ nm}$                       (c)  $100 \text{ nm}$                       (d)  $222 \text{ nm}$

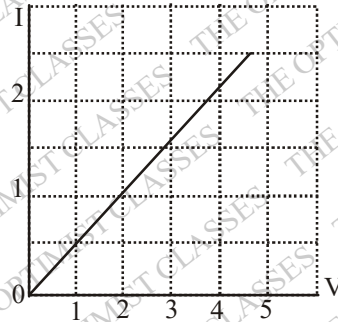
Q.10. A detector is used to count the number of  $\gamma$  rays emitted by a radioactive source. If the number of counts recorded in exactly 20 seconds is 10000, the error in the counting rate per second is

- (a)  $\pm 5.0$                       (b)  $\pm 22.4$                       (c)  $\pm 44.7$                       (d)  $\pm 220.7$

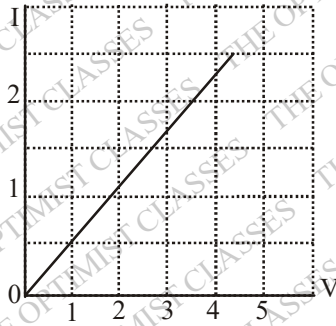
Q.11 Consider a standard chess board with  $8 \times 8$  squares. A piece starts from the left corner, which we call Square  $(1,1)$ . A single move of this piece corresponds to either one step right, i.e. to Square  $(1,2)$  or one step forwards, i.e., to Square  $(2,1)$ . If it continues to move according to these rules, the number of different paths by which the piece can reach the Square  $(5,5)$  starting from the Square  $(1,1)$  is

- (a) 120                      (b) 72                      (c) 70                      (d) 45

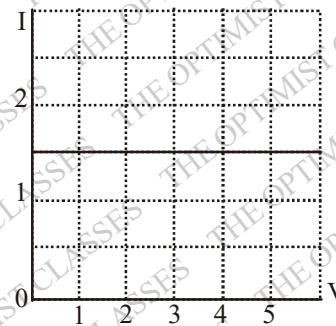
Q.12 The uppermost graph in the set below shows the variation of current  $i$  vs voltage applied across a copper conductor at temperature  $T_1$ . Which of the graph below -marked (a), (b), (c) or (d) - will show the possible variation of the I-V curve for the same conductor at another temperature  $T_2 > T_1$ ?



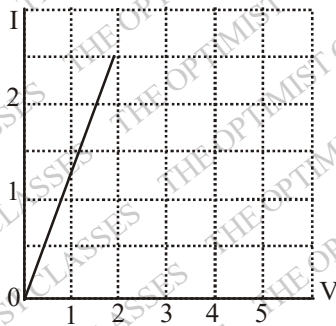
(a)



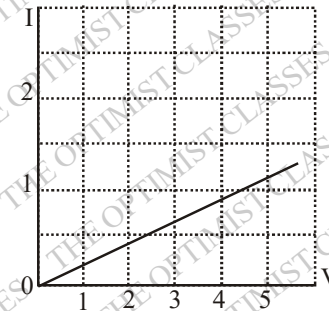
(b)



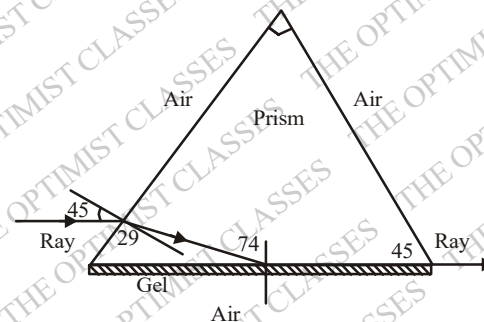
(c)



(d)



Q.13 A ray of light is incident on a right-angled prism as shown in the figure below. The lower surface of this prism is coated with a gel. If the incident ray makes an angle (marked in degrees) as shown in the figure refractive index of the gel must be



(a) 1.40

(b) 1.46

(c) 1.50

(d) 1.52

Q.14 A particle  $P_1$  is confined in one-dimensional infinite potential well with walls at  $x = \pm 1$ . Another particle  $P_2$  is confined in a one-dimensional infinite potential well with walls at  $x = 0, 1$ . Comparing the two particles, one can conclude that

(a) the no. of nodes in the  $n^{\text{th}}$  excited state of  $P_1$  is twice that of  $P_2$ .

(b) the no. of nodes in the  $n^{\text{th}}$  excited state of  $P_1$  is half that of  $P_2$ .

(c) the energy of the  $n^{\text{th}}$  level of  $P_1$  is the same as that of  $P_2$ .

(d) the energy of the  $n^{\text{th}}$  level of  $P_1$  is one quarter of that of  $P_2$ .

Q.15 A charged particle is in the ground state of a one-dimensional harmonic oscillator potential, generated by electrical means. If the power is suddenly switched off, so that the potential disappears, then according to quantum mechanics,

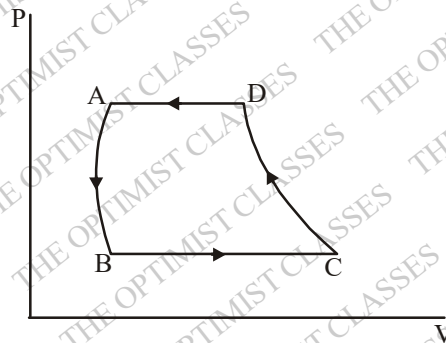
(a) the particle will shoot out of the well and move out towards infinity in one of the two possible directions

(b) the particle will stop oscillating and as time increases it may be found further and further away from the centre of the well

(c) the particle will keep oscillating about the same mean position but with increasing amplitude as time increases

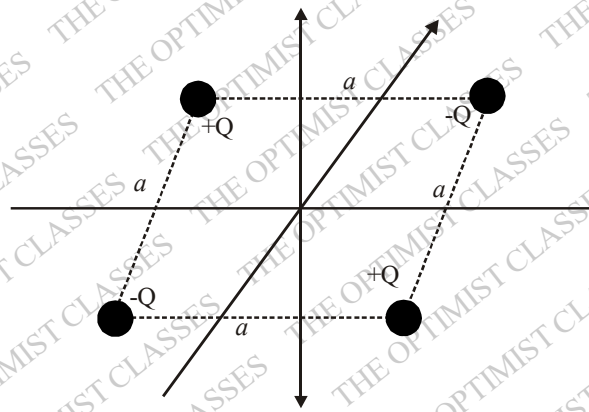
(d) the particle will undergo a transition to one of the higher excited states of the harmonic oscillator

Q.16 The  $pV$  diagram below represents a



(a) Carnot refrigerator (b) Carnot engine (c) gas turbine refrigerator (d) gas turbine engine

Q.17 In the laboratory, four point charges  $+Q, -Q, +Q, -Q$  are placed at the four ends of a horizontal square of side  $a$ , as shown in the figure below. The number of neutral points (where the electric field vanishes) is

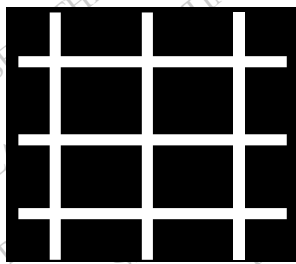
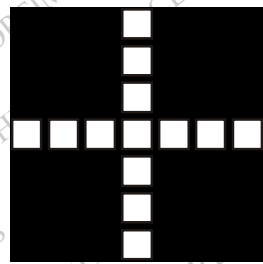
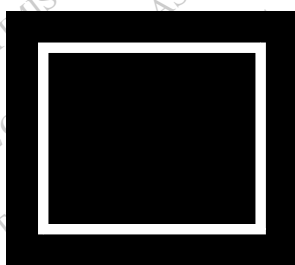
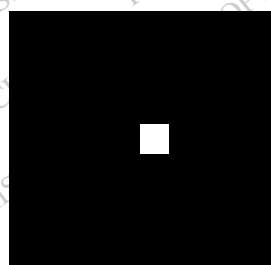


- (a)  $\infty$       (b) 4      (c) 1      (d) zero

Q.18 Coherent monochromatic light falling through a small aperture produced a Fraunhofer diffraction pattern as shown below

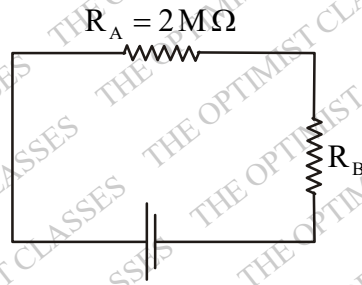


By looking at this diffraction pattern carefully one can guess that the shape of the aperture was

- (a)       (b) 
- (c)       (d) 

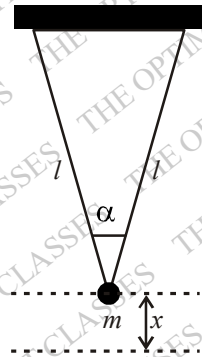
Q.19 In the circuit given below, a person measures 9.0 V across the battery, 3.0 V across the  $2M\Omega$  resistor  $R_A$  and 4.5 V across the unknown resistor  $R_B$ , using an ordinary voltmeter which has a finite input resistance  $r$ . Assuming that the battery has negligible internal resistance, it follows that (i) the resistance  $R_B$  and (ii) the input resistance  $r$  of the voltmeter are, in  $M\Omega$ ,





- (a)  $R_B = 3.0, r = 6.0$  (b)  $R_B = 2.5, r = 7.5$  (c)  $R_B = 4.0, r = 12.0$  (d)  $R_B = 4.5, r = 10.0$

Q.20 A heavy mass  $m$  is suspended from two identical steel wires of length  $l$ , radius  $r$  and Young's modulus  $Y$  as shown in the figure below. When the mass is pulled down by a distance  $x$  ( $x \ll l$ ) and released, it undergoes elastic oscillations in the vertical direction with a time period



- (a)  $\frac{2\pi}{r} \sqrt{\frac{ml}{2Y \cos^2(\alpha/2)}}$  (b)  $2\pi \sqrt{\frac{l \cos(\alpha/2)}{g}}$  (c)  $\sqrt{\frac{2\pi ml}{Yr^2}}$  (d)  $\frac{2\pi}{r} \sqrt{\frac{mgl}{2Y}}$

## SECTION :- B

**8 × 5 = 40 Marks**

Q.1 The wave function  $\psi$  of a quantum mechanical system described by a Hamiltonian  $\hat{H}$  can be written as a linear combination of  $\Phi_1$  and  $\Phi_2$  which are the eigenfunction of  $\hat{H}$  with eigenvalues  $E_1$  and  $E_2$  respectively. At

$t = 0$ , the system is prepared in the state  $\psi_0 = \frac{4}{5}\Phi_1 + \frac{3}{5}\Phi_2$  and then allowed to evolve with time. The wave

function at time  $T = \frac{1}{2} \frac{h}{(E_1 - E_2)}$  will be (accurate to within a phase)

- (a)  $\frac{4}{5}\Phi_1 + \frac{3}{5}\Phi_2$  (b)  $\Phi_1$  (c)  $\frac{4}{5}\Phi_1 - \frac{3}{5}\Phi_2$

(d)  $\Phi_2$       (e)  $\frac{3}{5}\Phi_1 + \frac{4}{5}\Phi_2$       (e)  $\frac{3}{5}\Phi_1 - \frac{4}{5}\Phi_2$

Q.2 Light transmitted along an optical fibre incurs losses due to Rayleigh scattering from inhomogeneities. If a fibre of given length transmits 50% of the monochromatic light coupled into it at a wavelength of 1330 nm, the transmitted fraction for the same fibre at 1550 nm will be

- (a) 55 %      (b) 57 %      (c) 62 %      (d) 67 %      (e) 74 %      (f) 87 %

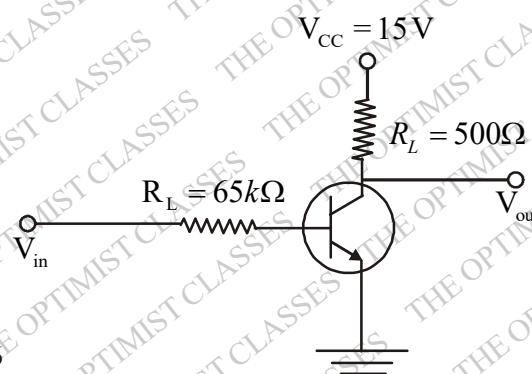
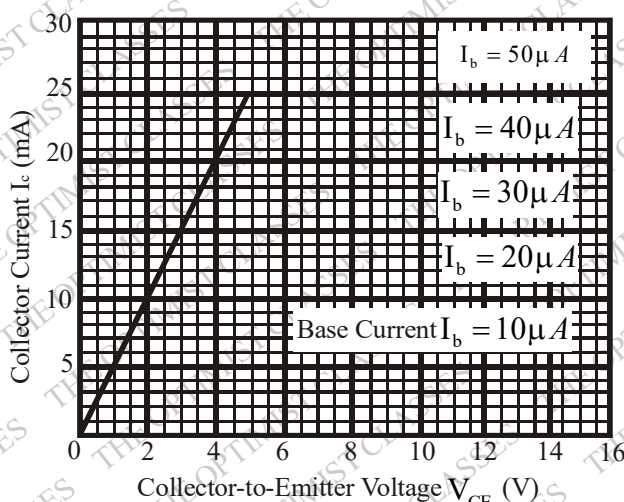
Q.3 A quantum system has three energy levels -0.12 eV, -0.2 eV and -0.44 eV respectively. Three electrons are distributed among these levels. At a temperature of 1727°C the system has total energy -0.68 eV. The free energy of the system is approximately

- (a) +1.5 eV      (b) +0.3 eV      (c) -0.1 eV      (d) -0.3 eV      (e) -1.0 eV      (f) -1.5 eV

Q.4 An atom is capable of existing in two states : a ground state of mass  $M$  and an excited state of mass  $M + \Delta$ . If the transition from the ground state to the excited state proceeds by the absorption of a photon, the photon frequency frame ( where the atom is initially at rest ) is

(a)  $\frac{\Delta c^2}{h}$       (b)  $\frac{\Delta c^2}{h} \left( 1 + \frac{\Delta}{2M} \right)$       (c)  $\frac{Mc^2}{h}$   
 (d)  $\frac{\Delta c^2}{h} \left( 1 - \frac{\Delta}{2M} \right)$       (e)  $\frac{Mc^2}{h} \left( 1 + \frac{\Delta}{2M} \right)$       (f)  $\frac{Mc^2}{h} \left( 1 - \frac{\Delta}{2M} \right)$

Q.5 A plot of the common-emitter characteristics of a silicon n-p-n transistor is shown below. Given this information and assuming that there will be a 0.7 V drop across a forward biased silicon p-n junction, the approximate value of the output voltage  $V_{out}$  for an input voltage  $V_{in} = 2$  V in the adjacent circuit will be



- (a) 4 V      (b) 6 V      (c) 8 V  
 (d) 10 V      (e) 12 V      (f) 14 V

Q.6 Measurement of the electric field ( $E$ ) and the magnetic field ( $B$ ) in a plane-polarized electromagnetic wave in vacuum led to the following :

$$\frac{\partial E}{\partial x} = \frac{\partial E}{\partial y} = 0,$$

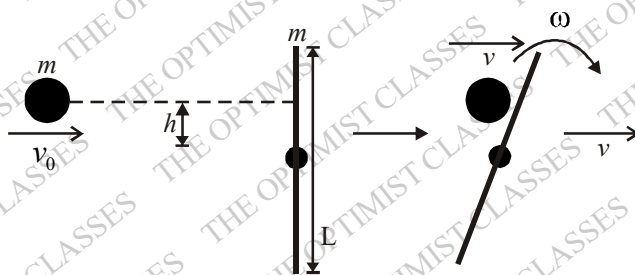
$$\frac{\partial E}{\partial z} = -\frac{\partial B}{\partial t} \quad \text{and} \quad \frac{\partial B}{\partial x} = \frac{\partial B}{\partial y} = 0,$$

$$\frac{\partial B}{\partial z} = \frac{\partial E}{\partial y}$$

It states that

- (a)  $\vec{E} = E\hat{i}, \vec{B} = B\hat{j}$  and the wave was travelling along  $\hat{k}$
- (b)  $\vec{E} = E\hat{j}, \vec{B} = B\hat{i}$  and the wave was travelling along  $\hat{k}$
- (c)  $\vec{E} = E\hat{j}, \vec{B} = B\hat{k}$  and the wave was travelling along  $-\hat{i}$
- (d)  $\vec{E} = E\hat{k}, \vec{B} = B\hat{i}$  and the wave was travelling along  $\hat{j}$
- (e)  $\vec{E} = E\hat{i}, \vec{B} = B\hat{k}$  and the wave was travelling along  $-\hat{j}$
- (f) the wave was travelling along  $\pm\hat{k}$  but direction of  $\vec{E}$  and  $\vec{B}$  are not uniquely defined.

Q.7 A mass  $m$  travels in a straight line with velocity  $v_0$  perpendicular to a uniform stick of mass  $m$  and length  $L$ , which is initially at rest. The distance from the centre of the stick to the path of the travelling mass is  $h$  (see figure). Now the travelling mass  $m$  collides elastically with the stick, and the centre of the stick and mass  $m$  are observed to move with equal speed  $v$  after the collision. Assuming that the travelling mass  $m$  can be treated as a point mass, and the moment of inertia of the stick about its center is  $I = \frac{mL^2}{12}$ , it follows that the distance  $h$  must be



- (a)  $\frac{L}{2}$
- (b)  $\frac{L}{4}$
- (c)  $\frac{L}{\sqrt{6}}$
- (d)  $\frac{L}{\sqrt{3}}$
- (e)  $\frac{L}{3}$
- (f) zero

Q.8 The binding energy per nucleon for  $^{235}\text{U}$  is  $7.6 \text{ MeV}$ . The  $^{235}\text{U}$  nucleus undergoes fission to produce two fragments, both having binding energy per nucleon  $8.5 \text{ MeV}$ . The energy released, in Joules, from the complete fission of  $1 \text{ Kg}$  of  $^{235}\text{U}$  is, therefore,

- (a) 8000
- (b)  $10^{35}$
- (c) 450
- (d) 20000
- (e)  $8.7 \times 10^{13}$
- (f)  $5.0 \times 10^8$