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# THE OPTIMIST CLASSES

AN INSTITUTE FOR NET-JRF/GATE/IIT-JAM/JEST/TIFR/M.Sc ENTRANCE EXAMS

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# TATA INSTITUTE OF FUNDAMENTAL RESEARCH (TIFR) PREVIOUS YEAR QUESTIONS

## **YEAR 2011**

- 1. Please fill-in details about name, reference code etc. on the question paper and answer sheet. Answer sheet is machine-readable. Read the instructions given on the reverse of the answer sheet before you start filling it up. Use only HB pencils to fill-in the answer sheet.
- 2. Indicate your ANSWER ON THE ANSWER SHEET by blackening the appropriate circle for each questions. *Do not mark more than one circle for any question*: this will be treated as a wrong answer.
- This test comes in two sections, **Section A** and **Section B**, both of which contain multiple choice-type questions. Only ONE of the options given at the end of each question is correct. Section A contains 20 questions, each with 4 options, and Section B contains 8 questions, each with 6 options. The maximum marks are 60 for section A plus 40 for Section B, totaling to 100. Marking shall be as:
  - (i) If the answer is **correct**: +3 marks in Section A: +5 marks in Section B.
  - (ii) If the answer is **incorrect**: -1 mark in both Section A & B.
  - (iii) If the answer is not attempted: 0 marks in both Section A & B.
  - (iv) If more than one box is marked: 0 marks in both Section A & B.
  - Note that negative marking as indicated above will be implemented.
- 4. As a rough guideline, the time spent on questions in Section A should be about 5 minutes each; questions in Section B should take about 10 minutes each. Obviously, some questions may take a little less time while others may require a little more.
- 5. We advise you to first mark the correct answer on the Question PAPER and then to TRANSFER these to the ANSWER SHEET only when you are sure of your choice.
- 6. Rough work may be done on blank pages of the question paper. If needed, you may ask for extra rough sheets from an invigilator.
- 7. **Use of calculators is permitted**. Calculator which plots graphs is NOT allowed. Multiple-use devices such as cell phones, smart phones etc., CANNOT be used for this purpose.
- 8. Do NOT ask for clarifications from the invigilators regarding the questions. They have been instructed not to respond any such inquiries from candidates. In case a Correction/clarification is deemed necessary; the invigilator(s) will announce it publicly.

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$$x + \frac{x^3}{3} + \frac{x^5}{5} + \frac{x^7}{7} + \dots$$

(a) 
$$\frac{1}{2} \ln \left[ (1+x)/(1-x) \right]$$

(b) 
$$\frac{1}{2} \ln \left[ (1-x)/(1+x) \right]$$

(c) 
$$\tan hx$$
 (d)  $\ln \left(1 - \frac{4}{\pi} \tan^{-1}x\right)$ 

- where  $-1 < x < \pm 1$ , can be summed to the value  $(a) \frac{1}{2} \ln \left[ (1+x)^{3} (1-x)^{3} \right] \qquad (b) \frac{1}{2} \ln \left[ (1-x)^{3} (1+x) \right] \qquad (c) \tan^{3} x$ A 100 page book is known to have 200 printing error hat one pages will be found to be only 13% A 100 page book is known to have 200 printing errors distributed randomly through the pages. The probability

$$M = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{pmatrix}$$

$$\begin{pmatrix}
2 \\
1 \\
-1
\end{pmatrix}, \begin{pmatrix}
1 \\
-1 \\
1
\end{pmatrix} and \begin{pmatrix}
0 \\
1 \\
-1
\end{pmatrix}$$

$$(b) \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix} \text{ and } \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}$$

$$(c) \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix} and \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}$$

$$(d) \begin{pmatrix} 2 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix} \text{ and } \begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix}$$

and the second state of t the same. Two solid spheres  $S_1$  and  $S_2$  of the same uniform density fall from rest under gravity in a viscous medium and, after some time, reach terminal velocities  $v_1$  and  $v_2$  respectively. If the masses of  $S_1$  and  $S_2$  are  $m_1$  and

 $m_2$  respectively, and  $v_1 = 4v_2$ , then the ratio  $\frac{m_1}{m_2}$  is

(a) 1/8 (b) 8 (c) 1/4

- TE OF TO Q.5 The ASSESSED REPORTED TO A SECOND REPO The dynamics of a particle of mass m is described in terms of three generalized coordinates Lagrangian of the system is

$$L = \frac{1}{8}m\left[\left(\zeta + \eta\right)\left(\frac{\dot{\zeta}^2}{\zeta^2} + \frac{\dot{\eta}^2}{\eta^2}\right) + 4\zeta\eta\dot{\varphi}^2\right] + \frac{1}{8}k\left(\zeta + \eta\right)^2$$

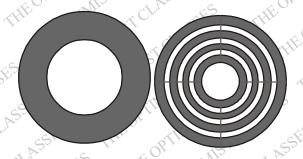
where k is a constant, then a conserved quantity in the system will be

(a)  $(m+k)(\dot{\zeta}+\dot{\eta})$ 

(b)  $m(\zeta + \eta)(\dot{\zeta}/\zeta^2 + \dot{\eta}/\eta^2)$ 

(c)  $m(\dot{\zeta}^2/\eta^2 + \dot{\eta}^2/\zeta^2)$ 

- $(d) m \zeta \eta \dot{\phi}$
- Q.6 A scientist is given two heavy spheres made of the same metal, which have the same diameter and weight, and is asked to distinguish the spheres, without damaging them in any way. Though the spheres look identical, one of them is actually a hollow spherical shell, while the other is a set of concentric shells mounted on four thin rods of the same metal (see figure).



To make this distinction, the scientist must perform an experiment where each sphere is

- (a) immersed fully in a non-corresive liquid and then weighed
- (b) made into the bob of the a long simple pendulum and set oscillating
- (c) set rotating under the action of a constant torque
- (d) given the same electric charge Q and the potential is measured
- Q.7 A narrow beam of light of wavelenght 589.3 nm from a sodium lamp is incident normally on a diffraction grating of transmission type. If the grating constant is  $10000000 \, m^{-1}$  the number of principal maxima observed in the transmitted light will be
  - (a) 1
- **(b)** 3

(c) 5

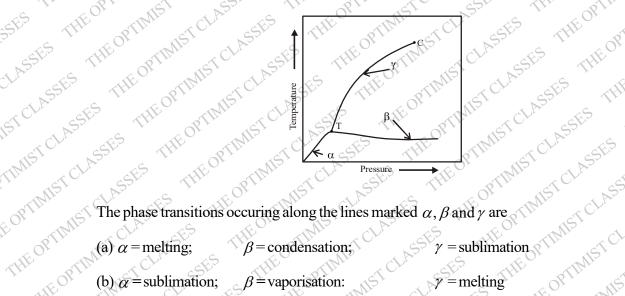
- (d) 7.0
- Q.8 A closed, thermally-insulated box contains one mole of an ideal monatomic gas G in thermodynamic equilibrium with blackbody radiation B. The total internal energy of the system is  $U = U_G + U_B$  where  $U_G$  and  $U_B (\propto T^4)$  are the energies of the ideal gas and the radiation respectively. If  $U_G = U_B$  at the temperature  $T_0K$ , then the energy required to raise the temperature from  $T_0K$  to  $(T_0 + 1)K$ , in terms of the gas constant R, is
  - (a) 0.33 R
- (b) 1.5 R
- (c) 6R
- (d) 7.5 R
- Q.9 The phase diagram of a pare substance is given in the figure below, where 'T' denotes the triple point and 'C' denotes the critical point.

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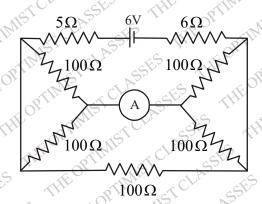
= sublimation rimits in the second

(a)  $\alpha = \text{melting};$  $\gamma = \text{melting}$ (b)  $\alpha$  = sublimation;  $\beta$  = vaporisation:

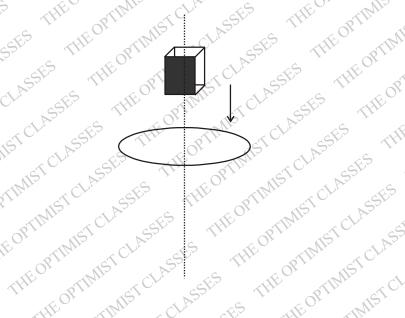
 $\gamma$  = condensation  $\beta$  = vaporisation; (c)  $\alpha = \text{melting}$ ;

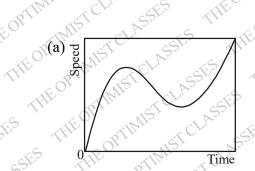
(d)  $\alpha$  = sublimation;  $\beta$  = melting;  $\gamma$  = vaporisation

The current read by the ammeter (A) in the circuit given below is

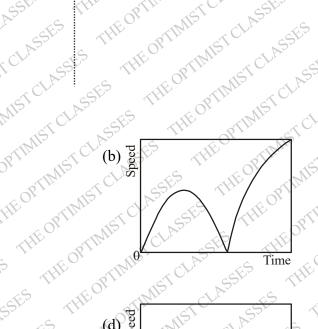


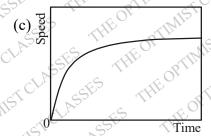
- THE OPTIMIST CLASSES (d) 54.5 mA (b) 100.0 mA (a) 50.0 mA (c) 27.3 mA
- ASSIQ.11 The sign of the majority charge carries in a doped silicon crystal is to be determined experimentally. In addition to a voltage supply the combination of instruments needed to perform the experiment is
  - (a) Thermometer, Voltmeter and Ammeter
  - (b) Magnet, Voltmeter and Ammeter
  - (c) Pickup Coil, Voltmeter and Ammeter
  - (d) Heater, Magnet and Thermometer
  - conducting wire, as shown in the figure below (on the left). The speed-versus-time graph, in arbitrary units of the magnet will corresponds most closely to which of the ferrollocal state of the ferrollocal state. Q.12 A small but very powerful magnet falls from the rest under gravity through the centre of a horizontal ring of the magnet will corresponds most closely to which of the four plots below(on the right)?

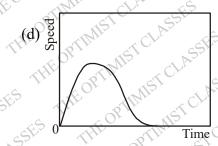




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- The spectra of electromagnetic radiation emitted by distant objects like stars and galaxies give important clues about their physical properties. In this context, a correct statement is that
  - (a) the wavelenghts in the emission of an element in a star are always the same as those found in laboratory experiments
  - (b) absorption spectra cannot be used to determine which molecules are present in the distant objects
  - (c) the nuclear structure of the distant objects cannot be determined from lines in the visible region of the
  - (d) absorption lines in the spectra of distant objects do not carry information about their motion in a direction trasverse to the line of sight trasverse to the line of sight
- Given that the ionization energies of Hydrogen  $\binom{1}{H}$  and Lithium  $\binom{3}{Li}$  are 13.6 eV and 5.39 eV, respectively

the effective nuclear charge experience by the valence electron of a  $^3Li$  atom may be estimated in terms of the proton charge e as

- (a) 3.00 e
- (c) 1.26 e
- (d) 0.63 e

Two identical non-interacting particles, each of mass m and spin  $\frac{1}{2}$ , are placed in a one-dimensional box of

lenght L. In quantum mechanics, the lowest possible value of the total energy of these two particles is  $\varepsilon_0$ . If instead, four such particles are introduced into a similar one-dimensional box of length 2L, then the lowest possible value of their total energy will be

- (c)  $3\varepsilon_0$

An excited atomic electron undergoes a spontaneous transition

$$3d_{3/2} \rightarrow 2p_{1/2}$$

The interaction responsible for this transition must be of the type (a) electric dipole (E1).

magnetic dipole (M1)

- (b) electric quadrupole (E2)

(c) electric quadrupole (E2)

(d) electric dipole (E1)

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magnetic quadrupole (M2) magnetic quadrupole (M2)

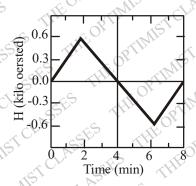
A fast-moving  $^{14}$  N nucleus collides with an  $\alpha$  particle at rest in the laboratory frame, giving rise to the reaction

$$^{14}N + \alpha \rightarrow ^{17}O + p$$

Given the masses 14.00307 a.m.u. and 16.99913 a.m.u. for  $^{14}$  N and  $^{17}$  O nuclei respectively, and 4.00260 a.m.u. and 1.00783 a.m.u. for  $\alpha$  and p respectively, the minimum kinetic energy in the laboratory frame of the <sup>14</sup> N nucleus must be

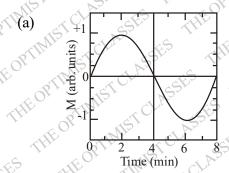
- (a) 1.20 *MeV*
- (b) 1.55 *MeV*
- (c) 4.20 MeV
- (d) 5.41 MeV

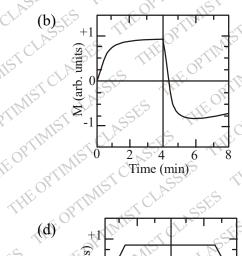
An unmagnetised sample of iron is placed in a magnetic field H which varies with time as shown in the plot

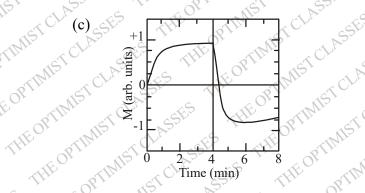


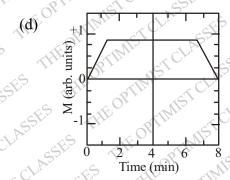
The magnetization M of the iron sample is continuously measured and also plotted as a function of time. The

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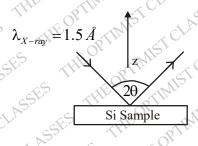


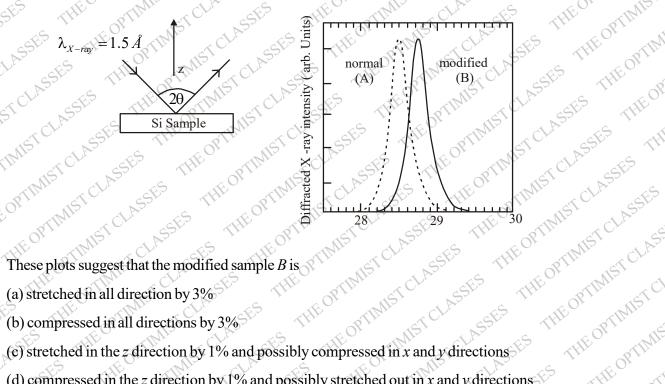






The figure below shows the Bragg diffraction pattern for X-rays of wavelength 1.54  $\mathring{A}$  incident on two crystalline Silicon thin film Sample A and B. The dashed line corresponds to a normal Sample A and the continue line corresponds to another Sample B, which is modified due to differences in the growth conditions.



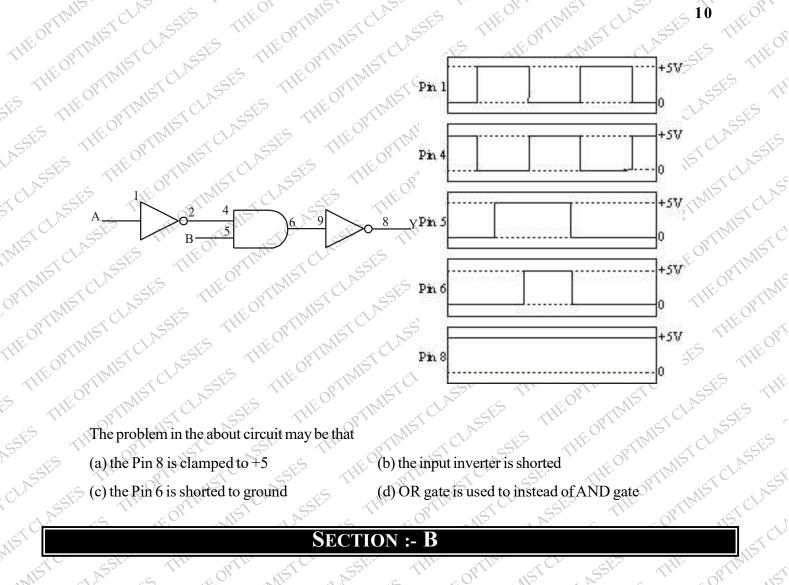


- These plots suggest that the modified sample *B* is

  (a) stretched in all direction by 3%

  (b) compressed in all directions by 3%

  (c) stretched in the *z* direction by 1% and possibly compressed in *x* and *y* directions
- Q.20 The digital electronic circuit below (left side) has some problem and is not performing as intended. The voltage at each pin as a function of time is shown in the adjacent figures.



- (b) the input inverter is shorted
- (c) the Pin 6 is shorted to ground

(c) the Pin 6 is shorted to ground (d) OR gate is used to instead of AND gate

SECTION:-B

$$8 \times 5 = 40 \text{ MARKS}$$
Q.1 The trace of the real  $4 \times 4$  matrix  $U = \exp(A)$ , where

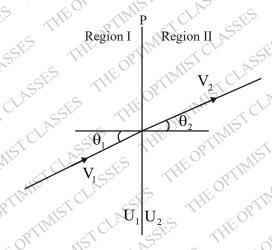
$$A = \begin{bmatrix}
0 & 0 & 0 & \pi/4 \\
0 & 0 & \pi/4 & 0 \\
0 & \pi/4 & 0 & 0
\\
-\pi/4 & 0 & 0 & 0
\end{bmatrix}$$
is equal to

(a) 2 (b)  $\pi/4$  (c)  $\exp(i\varphi)$  for  $\varphi = 0, \pi$ 

(d) zero (e)  $\pi/2$  (f)  $2\sqrt{2}$ .

Q.2 Aregion of space is divided into two parts by a plane P, as shown in the figure below. A particle of mass  $m$ 

- (a) 2 (b)  $\pi/4$  (c)  $\exp(i\varphi)$  for  $\varphi=0,\pi$  (d) zero (e)  $\pi/2$  (f)  $2\sqrt{2}$ Q.2 Aregion of space is divided into two parts by a plane P, as shown in the figure below. A particle of mass m passes from Region I and Region II where it has speed  $\nu_1$  and  $\nu_2$  respectively. There is a constant potential  $U_1$  in Region I and  $U_2$  in Region II.



Let T<sub>1</sub> be the kinetic energy of the particle in Region I. If the trajectory of the particle is inclined to the normal to the plane P by angles  $\theta_1$  and  $\theta_2$ , as shown in the figure then the ratio  $\sin \theta_1 / \sin \theta_2$  is given by

(a) 
$$\sqrt{1-T_1/(U_1-U_2)}$$

(b) 
$$\sqrt{1+T_1/(U_1-U_2)}$$

(c) 
$$\sqrt{1+(U_1-U_2)/T_1}$$

(d) 
$$\sqrt{1+(U_1+U_2)/T_1}$$

(e) 
$$\sqrt{1-T_1(U_1-U_2)}$$

(f) 
$$\sqrt{1-(U_1-U_2)/T_1}$$

The electric field of an electromagnetic wave of angular frequency  $\omega$  propagating in a medium with conductivity  $\sigma$ , paermitivity  $\varepsilon$  and permeability  $\mu$  is given by

$$E = E_0 \exp\left[-i\left(\omega t - kx\right)\right]$$

where the imaginary part of the complex propagation constant k is  $\omega\sqrt{\mu\varepsilon/2}$  multiplied by the factor

(a) 
$$\sqrt{1+\sqrt{\sigma/\omega\varepsilon}}+1$$

(b) 
$$\left[\sqrt{1+\sigma/\omega\varepsilon}+1\right]^{1/2}$$

(c) 
$$\left[\sqrt{1+\left(\sigma/\omega\varepsilon\right)^2}+1\right]^{1/2}$$

the complex propagation constant 
$$k$$
 is  $\omega \sqrt{\mu \varepsilon / 2}$  multiplication (b)  $\left[ \sqrt{1 + \sigma / \omega \varepsilon} + 1 \right]^{1/2}$  (d)  $\left[ \sqrt{1 + (\sigma / \omega \varepsilon)^2} - 1 \right]^{1/2}$ 

(e) 
$$\left[\sqrt{1+\sqrt{\sigma/\omega\varepsilon}}-1\right]^{1/2}$$

$$(f) \left[ \sqrt{1 + \sigma / \omega \varepsilon} - 1 \right]^{1/2}$$

A system having N non-degenerate energy eigenstates is populated by N identical spin-zero particles and 2N identical spin-half particles. There are no interactions between any of these particles. If N = 1000, the entropy

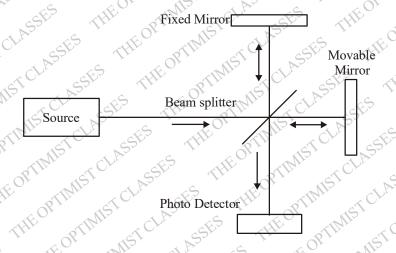
(b)  $1000 k_B$ 

(c) 13.82  $k_B$ 

(e) 5909.693  $k_B$ 

(f) 6909  $k_B$ 

(d)  $693.1 k_B$ The Michelson interferometer in the figure below can be used to study properties of light emitted by distant sources.



A Source  $S_1$ , when at rest, is known to emit light of wavelenght 632.8 nm. In this case, if the Movable mirror is translated through a distance d, it is seen that 99,565 interference fringes pass across the Photo-Director. For another source  $S_2$ , moving at an uniform speed of  $1.5 \times 10^7$  ms<sup>-1</sup> towards the interferometer along the straight line joining it to the Beam Splitter, one sees 100,068 interference fringes pass across the Photo-Detector for the same displacement d of the Movable Mirror. It follows that  $S_2$ , in its own rest frame, must be emitting light of wavelenght

(a) 599.6 nm

(b) 598.6 nm

(c) 628.0 nm

(d) 631.2 nm

- (e) 661.9 nm
- (f) 662.8 nm

Q.6 A particle oaf mass m is placed in the ground state of a one dimensional harmonic ocillator potential of the form

$$V(x) = \frac{1}{2}kx^2$$

where the stiffness constant k can be varied externally. The ground state wavefunction has the form  $\psi(x) \propto \exp\left(-ax^2\sqrt{k}\right)$  where a is a constant. If suddenly, the parameter k is changed to 4k, the probability that the particle will remain in the ground state of the new potential is

A Cloud Chamber of width 0.01 m is filled with pure nitrogen gas  $(N_2)$  at normal temperature and pressure. A beam of  $\alpha$  particles, when incident normally on the chamber, makes tracks which are visible under strong illumination. Whenever an  $\alpha$  particle  $\frac{4}{2}$ He has a nuclear collision with a  $\frac{14}{7}$ N nucleus, the track shows a distinct bend. The radius of a nucleus is given by  $r = r_0 A^{1/3}$  where  $r_0 = 1.217 \times 10^{-5} m$  and A is the atomic mass number.

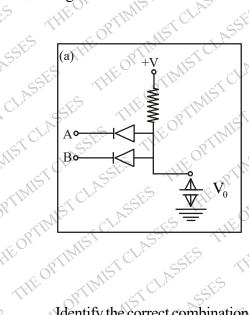
If the  $\alpha$  particles move at non-relativistic speeds and the total number of incident of  $\alpha$  particles is  $10^7$ , the number of such distinct bends is approximately

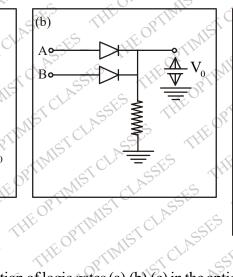
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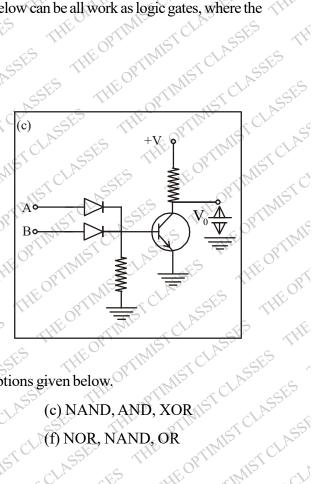
(d) 400

(e) 500

- (f) 600 CLAS
- THE OPTIMIS The three electronic circuits marked (i), (ii) and (iii) in the figure below can be all work as logic gates, where the input OPTIMIST CLASSES THE OPTIMIST CLA input THE OPTIMI signals are either 0V or 5V and the output is  $V_0$ .







en below, Orthonson, (c) NAND, AND, XO,
(d) NAND, AND, XO,
(e) NAND, AND, XO,
(f) NOR, NAND, OR
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