OPTIMIST CLASSES IIT-JAM TOPPERS



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THE OPTIMIST CLASSES

AN INSTITUTE FOR NET-JRF/GATE/IIT-JAM/JEST/TIFR/M.Sc ENTRANCE EXAMS

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TATA INSTITUTE OF FUNDAMENTAL RESEARCH (TIFR) PREVIOUS YEAR QUESTIONS

YEAR 2013

Name:- Date:- Date:-

- 1. Please fill-in details about name, reference code etc. on the question paper and answer sheet. Answer sheet is machine-readable. Read the instructions given on the reverse of the answer sheet before you start filling it up. Use only HB pencils to fill-in the answer sheet.
- 2. Indicate your ANSWER ON THE ANSWER SHEET by blackening the appropriate circle for each questions. *Do not mark more than one circle for any question*: this will be treated as a wrong answer.
- 3. This test comes in two sections, **Section A** and **Section B**, both of which contain multiple choice-type questions. Only ONE of the options given at the end of each question is correct. Section A contains 20 questions, each with 4 options, and Section B contains 8 questions, each with 4 options. The maximum marks are 60 for section A plus 40 for Section B, totaling to 100. Marking shall be as:
 - (i) If the answer is **correct**: +3 marks in Section A: +5 marks in Section B.
 - (ii) If the answer is **incorrect**: -1 mark in both Section A & B.
 - (iii) If the answer is not attempted: 0 marks in both Section A & B.
 - (iv) If more than one box is marked: 0 marks in both Section A & B.
 - Note that negative marking as indicated above will be implemented.
- 4. As a rough guideline, the time spent on questions in Section A should be about 5 minutes each; questions in Section B should take about 10 minutes each. Obviously, some questions may take a little less time while others may require a litle more.
- 5. We advise you to first mark the correct answer on the Question PAPER and then to TRANSFER these to the ANSWER SHEET only when you are sure of your choice.
- 6. Rough work may be done on blank pages of the question paper. If needed, you may ask for extra rough sheets from an invigilator.
- 7. **Use of calculators is permitted**. Calculator which plots graphs is NOT allowed. Multiple-use devices such as cell phones, smart phones etc., CANNOT be used for this purpose.
- 8. Do NOT ask for clarifications from the invigilators regarding the questions. They have been instructed not to respond any such inquiries from candidates. In case a Correction/clarification is deemed necessary; the invigilator(s) will announce it publicly.

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SECTION :- A

To be attempted by ALL candidates

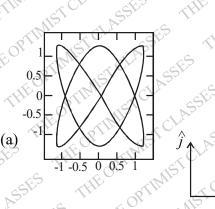
The value of the integral

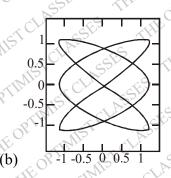
$$\int_{0}^{\infty} dx x^{9} \exp\left(-x^{2}\right) \mathrm{ds}$$

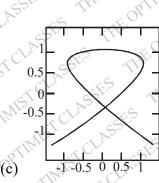
- (a) 20160
- (b) 24
- THE OPTIMIST CLASSES (d) 12 5 15 5
- A two-dimensional vector $\vec{A}(t)$ is given by

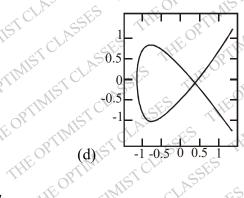
$$\vec{A}(t) = \hat{i}\sin 2t + \hat{j}\cos 3t$$

Which of the following graphs best describes the locus of the tip of the vector, as t is varied from 0 to 2π ?









- $\frac{dy}{dx} + y = 0$ has the complete solution, in terms of arbitrary constant A and B The differential equation
 - (a) $A \exp x + B \exp(-x)$

(b) $A \exp x + Bx \exp(-x)$

(c) $x\{A\exp x + B\exp(-x)\}$

- (d) $A \exp x + Bx \exp x$
- A stone is dropped vertically from the top of a tower of height 40m. At the same time a gun is aimed directly at the stone from the ground at a horizontal distance 30m from the base of the tower and fired. If the bullet from the gun is to hit the stone before it reaches the ground, the minimum velocity of the bullet must be, approximately, (a) 57.4 ms⁻¹
- (b) 27.7 ms⁻¹

- $(c) 17.7 \text{ ms}^{-1}$

Q5. Consider the uniform solid right cone depicted in the figure on the right. This cone has mass M and a circular base of radius r. If the moment of inertia of the cone about an axis passing through the centre of mass $O_{C.M.}$ (see figure) is given by

$$\frac{3}{80}M\left(4r^2+h^2\right)$$

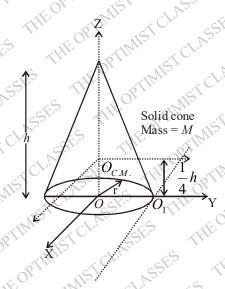
then the moment of inertia about another axis parallel to the X axis, but passing through the point O (see figure), is

(a)
$$\frac{3}{80}M(4r^2+h^2)$$

$$(b)\frac{1}{20}M(23r^2+2h^2)$$

$$(c)\frac{3}{40}M(2r^2+h^2)$$

$$(d)\frac{1}{30}M(15r^2+4h^2)$$



Q6. Two planets A and B move around the Sun in elliptic orbits with time periods T_A and T_B respectively. If the eccentricity of the orbit of B is ε and its distance of closest approach to the Sun is R, then the maximum possible distance between the planets is

Eccentricity of an ellipse:
$$\varepsilon = \frac{r_{\text{max}} - r_{\text{min}}}{r_{\text{max}} + r_{\text{min}}}$$

(a)
$$\frac{1+\varepsilon^2}{1-\varepsilon^2} \left(1 + \frac{T_A^{3/2}}{T_B^{3/2}} \right) R$$

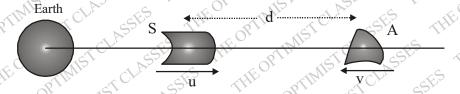
(b)
$$\sqrt{\frac{1+\varepsilon^2}{1-\varepsilon^2}} \left(1 + \frac{T_A^{2/3}}{T_B^{2/3}}\right) R$$

(c)
$$\sqrt{\frac{1+\varepsilon}{1-\varepsilon}} \left(1 + \frac{T_A^3}{T_B^3}\right) R$$

A spaceship S blasts off from the

(d)
$$\frac{1+\varepsilon}{1-\varepsilon} \left(1 + \frac{T_A^{2/3}}{T_B^{2/3}} \right) R$$

Q7. A spaceship S blasts off from the Earth. After some time, Earth station informs the crew that they have settled into a constant velocity 0.28c radially outward from the Earth, but unfortunately they are on a head-on collision course with an asteroid A at a distance of 15 light-minutes coming in towards the Earth along the same radius (see figure below).

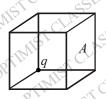


Instruments on-board the spaceship immediately estimate the speed of the asteroid to have a constant value 0.24c. It follows that the maximum time (in minutes) available to the crew to evacuate the ship before the collision is

- (a) 29
- (b) 30
- (c) 60

(d) 63

A point charge q sits at a corner of a cube of side a, as shown in the figure on the right. The flux of the electric field vector through the shaded side (region A) is



(a)
$$\frac{q}{24\varepsilon_0}$$

$$(b)\frac{q}{16\varepsilon_0}$$

$$(c)\frac{q}{8\varepsilon_0}$$

$$(d)\frac{q}{6\varepsilon_0}$$

A parallel plate capacitor of circular cross section with radius r >> d, Where 'd' is the spacing between the plates, is charged to a potential V and then disconnected from the charging circuit. If, now, the plates are slowly pulled apart (keeping then parallel) so that their separation is increased from d to d', the work done will be

(a)
$$\frac{\pi \varepsilon_0 r^2 V^2}{2d} \left(1 - \frac{d}{d!} \right)$$

(a)
$$\frac{\pi \varepsilon_0 r^2 V^2}{2d} \left(1 - \frac{d}{d'} \right)$$
 (b) $\frac{\pi \varepsilon_0 r^2 V^2}{2d} \left(\frac{d'}{d} - 1 \right)$ (c) $\frac{\pi \varepsilon_0 r^2 V^2}{2d} \frac{d'}{d}$

(c)
$$\frac{\pi \varepsilon_0 r^2 V^2}{2d} \frac{d'}{d}$$

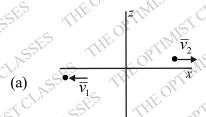
(d)
$$\frac{\pi \varepsilon_0 r^2 V^2}{2d} \frac{d}{d}$$

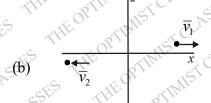
respectively, but not along the same straight line as shown below. In the laboratory frame two electrons are shot at each other with equal and opposite velocities \vec{u}_1 and \vec{u}_2

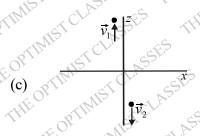


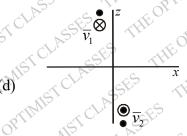
Each electron will be acted on by the Coulomb repulsion due to the other, as well as the Lorentz force due to its own motion in the magnetic field created by the other. Which of the diagrams given below best describes the final velocities \overline{v}_1 and \overline{v}_2 of these electrons?

[You may assume that the electrons are distinguishable.]









- A certain amount of fluid with heat capacity C_E Joules/°C is initially at a temperature 0°C. It is then brought into contact with a heat bath at a temperature of 100°C, and the system is allowed to come into equilibrium. In this process, the entropy (In Joules /°C) of the Universe changes by (a) $100 C_{F}$ (b) 0.044 C_{F}
- Q12. A monoatomic gas is described by the equatiion of state

$$p(V-bn)=nRT$$

where b and R are constants and other quantities have their usual meanings.

The maximum density (in moles per unit volume) to which this gas can be compressed is

	1
(a)	$\frac{-}{h}$

(c)
$$\frac{1}{bn}$$

(d) infinity In a quantum mechanical system, an observable A is represented by an operator \hat{A} . If $|\psi\rangle$ is a state of the system, but not an eigenstate of \hat{A} , then the quantity $r = \langle \psi \, | \, \hat{A} \, | \psi \, \rangle^2 - \langle \psi \, | \, \hat{A}^2 \, | \psi \, \rangle$

$$r = \langle \psi | \hat{A} | \psi \rangle^2 - \langle \psi | \hat{A}^2 | \psi \rangle$$

satisfies the relation

(a)
$$r > 0$$

(b)
$$r = 0$$

(c)
$$r < 0$$

(d)
$$r \le 0$$

Consider a quantum mechanical system with three linear operators \hat{A} , \hat{B} and \hat{C} , which are related by $\hat{A}\hat{B}-\hat{C}=\hat{I}$

$$\hat{A}\hat{B} - \hat{C} = \hat{I}$$

Where \hat{j} is the unit operator. If $\hat{A} = \frac{d}{dx}$ and $\hat{B} = x$, then \hat{C} must be

(a) Zero

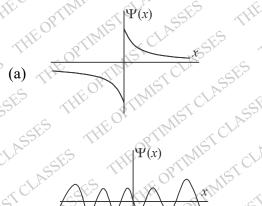
(b) $\frac{d}{dx}$ (c) $x \frac{d}{dx}$

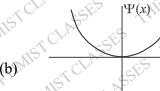
(b)
$$\frac{d}{dx}$$

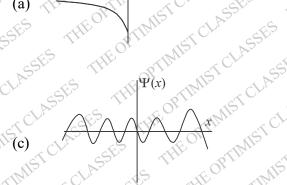
(c)
$$x \frac{d}{dx}$$

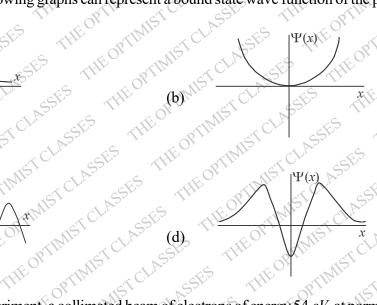
(d)
$$-x\frac{d}{dx}$$

of a potential wave five (a) Zero (b) $\frac{d}{dx}$ (c) $x\frac{d}{dx}$ (d) $-x\frac{d}{dx}$ A particle of energy E moves in one dimension under the influence of a potentials V(x). If E > V(x) for some range of x, which of the following graphs can represent a bound state wave function of the particle?









- In a Davisson Germer experiment, a collimated beam of electrons of energy 54 eV, at normal incidence on a given crystal, shows a peak at a reflection angle of 40°. If the electron beam is replaced by a neutral beam, and the peak appears at the same value of reflection angle, then the energy of the neutrons must be
 - (a) 33 eV
- (b) 0.03 eV
- (c) 0. eV
- The velocity of an electron in the ground state of a hydrogen atom is v_H . If v_P be the velocity of an electron (c) $v_P = \frac{v_H}{2}$ in the ground state of positronium, then

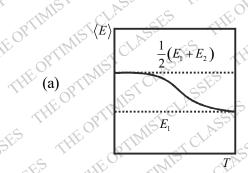
- Consider an ensemble of microscopic quantum mechanical systems with two energy levels E_1 and E_2 , where $E_1 < E_2$. Which of the following graphs best describes the temperature dependence of the average energy $\langle E \rangle$ of the system?

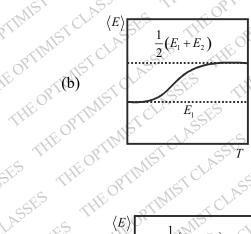
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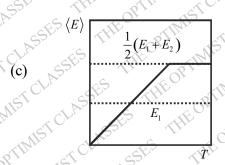
THE OPTIMIST CLASSES

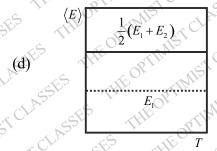
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A ray of light is incident on the surface of a thin prism at a small angle θ_1 with the normal, as shown in the figure on the right. The material of the prosm has refractive index n and you may assume the outside refractive index oetween t.

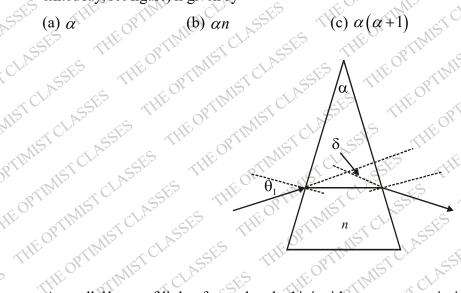
(d) $\alpha(\alpha-1)$ THE OPTIMIST CLASSES to be unity. If the (small) apex angle of the prism is α , the deviation angle δ (angle between the incident and exited ray; see figure) is given by

(a)
$$\alpha$$

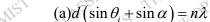
(b)
$$\alpha n$$

(c)
$$\alpha(\alpha+1)$$

(d)
$$\alpha(\alpha-1)$$



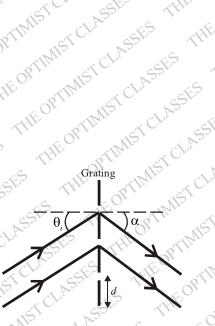
A parallel beam of light of wavelenght λ is incident on a transmission grating with groove spacing d, at an angle θ_i , as shown in the figure. The plane of incidence is normal to the grooves. After diffraction, the transmitted beam is seen to be at an angle relative to the normal. Which of the following conditions must be satisfied for this to happen?



(b)
$$d(\sin\theta_i - \sin\alpha) = n\lambda$$

(c)
$$2d \sin(\theta_i - \alpha) = n\lambda$$

$$(d)2d\sin(\theta_i + \alpha) = n\lambda$$



THE OPTIMIST CLASSES

- Q21 Let E_N be the energy released when one mole of pure U^{235} undergoes controlled fission, and E_C be the energy released when one mole of pure carbon undergoes complete combustion. The ration E_N/E_C will have the order TLASSES (d) 106 OPTIMES of magnitude
 - (a) 10⁴
- (c) 10^9
- The entropy S of a black hole is known to be of the form

$$S = \alpha k_B A$$

where A is the surface area of the black hole and α is a constant, which can be written in terms of c (velocity of light in vacuum), \hbar (reduced Planck's constant) and G_N (Newton's constant of gravitation). Taking the it follows that the entropy S is $R = \frac{2G_N M}{c^2}$ (a) $\frac{G_N^2 M^2 k_B}{2I^2}$ radius of the black hole as

$$R = \frac{2G_N M}{c^2}$$

- $(d) \frac{G_N M^2 k_B}{\lambda h^2}$

[λ is a numerical constant]

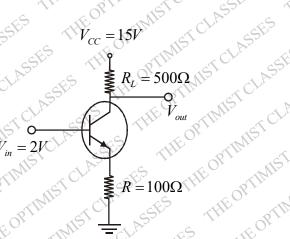
silicon n-p-n transistor.

(b) $\frac{\hbar c k_B}{\lambda G_N M}$ (c) $\frac{G_N^2 M^2 k_B}{\lambda \hbar c^4}$ (d) $\frac{G_N M}{\lambda \hbar}$ [λ]

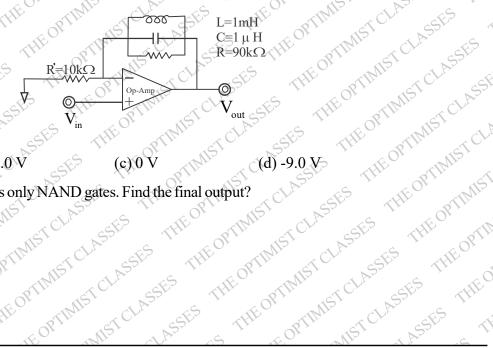
The circuit depicted on the right has been made with a silicon n-p-n transistor.

Assuming that there will be a 0.7 V drop acresiased silicon p-n junction, the power ansistor will be, approximately approximatel

- (b) 94 mW
- (c) 17 mW
 - (d) 67 mW

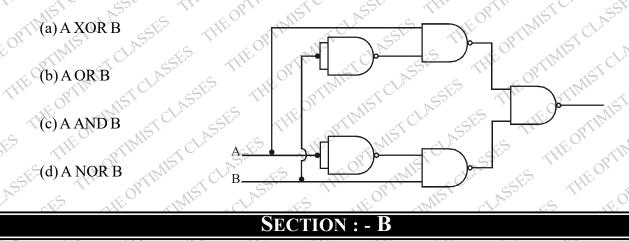


An input of 1.0 V DC is given to the ideal OP-Amp circuit depicted below. What will be the output voltage?



- Printer Q25. The ci (a) $10.0\,\mathrm{V}$ (b) $1.0\,\mathrm{V}$ (c) $0\,\mathrm{V}$ (d) -9.0 V The circuit shown below uses only NAND gates. Find the final output? THE OPTIMIST CLASS

- EON A XOR B THE (b) A OR B



To be attempted only by candidates for Integrated Ph.D. programme

(Candidate for Ph.D. programme will get no credit for attempting this section.)

$$4x^2 + v^2 + z = 0$$

(a)
$$-\frac{1}{\sqrt{5}}\hat{i} + \frac{3}{\sqrt{5}}\hat{j} - \frac{4}{\sqrt{5}}\hat{k}$$

(b)
$$\frac{1}{5}\hat{j} - \frac{4}{5}\hat{k}$$

(c)
$$\frac{4}{9}\hat{i} - \frac{8}{9}\hat{j} + \frac{1}{9}\hat{k}$$

(d)
$$\frac{1}{\sqrt{5}}\hat{i} = \frac{2}{\sqrt{5}}\hat{j}$$

Q26. Consider the surface corresponding to the equation $4x^2 + y^2 + z = 0$ A possible unit tangent to this surface at the point (1, 2, -8) is $(a) -\frac{1}{\sqrt{5}}\hat{i} + \frac{3}{\sqrt{5}}\hat{j} - \frac{4}{\sqrt{5}}\hat{k}$ $(b) \frac{1}{5}\hat{j} - \frac{4}{5}\hat{k}$ $(c) \frac{4}{9}\hat{i} - \frac{8}{9}\hat{j} + \frac{1}{9}\hat{k}$ $(d) \frac{1}{\sqrt{5}}\hat{i} - \frac{2}{\sqrt{5}}\hat{j}$ Q27. A particle with time-varying mass $m(t) = m_0 \left(1 - \frac{t}{\tau}\right)$, where m_0 and τ are positive constants, moves along the x-axis under the action of a constant positive force F for 0 < t < -1 If the particle is t = -1. τ are positive constants, moves along the x-axis under the action of a constant positive force F for $0 \le t \le \tau$. If the particle is at rest at time t = 0, then at time t = t, its velocity v will be at time t = t, its velocity v will be Q28. A ball of mass m slides up J friction.

(a)
$$-\frac{\tau F}{m_0} \log \left(1 - \frac{t}{\tau} \right)$$

(b)
$$-\frac{Ft}{m_0}\log\frac{t}{\tau}$$

(c)
$$\frac{Ft}{m_0} \left(1 - \frac{t}{\tau}\right)^{-1}$$

$$(d)\frac{\tau F}{m_0} \left(1 - \frac{t}{\tau} \right)$$

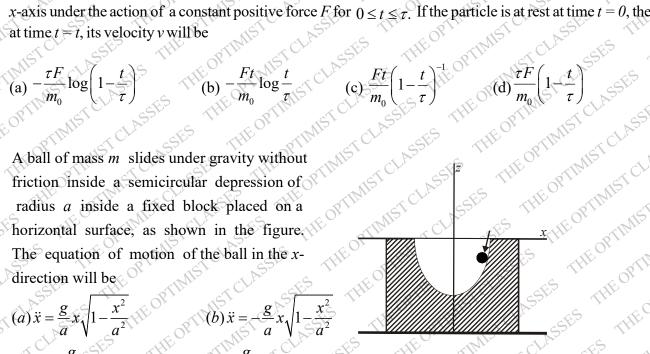
(b) $-\frac{Ft}{m_0}\log\frac{t}{\tau}$ (c) $\frac{Ft}{m_0}\left(1-\frac{t}{\tau}\right)^{-1}$ (d) $\frac{\tau}{m}$ A ball of mass m slides under gravity without friction inside a semicircular depression of radius a inside a fixed block placed on a horizontal surface, as shown in t^1 . The equation of most irection t^2 .

$$(a)\ddot{x} = \frac{g}{a}x\sqrt{1 - \frac{x^2}{a^2}}$$

$$(b)\ddot{x} = -\frac{g}{a}x\sqrt{1 - \frac{x^2}{a^2}}$$

$$(c)\ddot{x} = -\frac{g}{a}x$$

$$(d)\ddot{x} = \frac{g}{a}.$$



Q29. A particle P, of rest mass M and energy E, suddenly decays into two particles A and B of rest masses m_A and m_B respectively, and both particles move along the straight line in which P was moving. A possible energy E_A of the particle A will be

(a)
$$\frac{E}{2} \left\{ 1 + \left(\frac{m_A - m_B}{M} \right)^2 \right\}$$

(b)
$$\frac{E}{2} \left\{ 1 - \left(\frac{m_A^2 - m_{\tilde{B}}^2}{M^2} \right) \right\}$$

(c)
$$\frac{E}{2} \left\{ 1 + \left(\frac{m_A + m_B}{M} \right)^2 \right\}$$

(d)
$$\frac{E}{2} \left\{ 1 + \left(\frac{m_A^2 - m_B^2}{M^2} \right)^2 \right\}$$

Q30. Consider two charges +Q and -Q placed at the point (a, 0) and (-a,0) in a plane, as shown in the figure on the right. If the origin is moved to the point (X, Y), the magnitude of the dipole moment of the given charge distribution with respect to this origin will be



(c)
$$Q(a-X)-Q(-a+X)$$

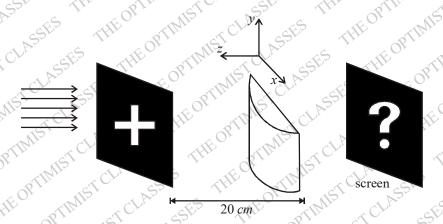
$$(d) 2Qa\sqrt{X^2 + Y^2}$$

Q31. A plane electromagneite wave travelling in a vacuum is characterised by the electric and magneite fields

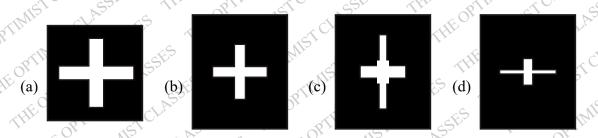
$$\vec{E} = \hat{i} \left(30\pi \, \text{Vm}^{-1} \right) \exp i \left(\omega t + kz \right); \, \vec{H} = \hat{j} \left(H_0 \, \text{Am}^{-1} \right) \exp i \left(\omega t + kz \right)$$

If ω , k > 0, The value of H_0 must be

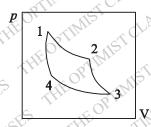
- (a) 2π
- (b) 0.67
- (c) 0.25
- (d) 0.94
- Q32. Which of the following classic experiments provides unambiguous proof that the Earth is a non-inertial frame of reference with respect to the fixed stars?
 - (a) Fizeau's rotating wheel experiment
- (b) Michelson Morley experiment
- (c) Foucault's pendulum experiment
- (d) Newton's coin and feather experiment
- Q33. A cross-shaped opening is illuminated by a parallel beam of white light. A thin plano convex cylindrical glass lens is placed 20 *cm* in front of it, as shown in the figure below



The radius of curvature of the curved surface of the lens is 5 cm and 1.5 is the refractive index of glass. On a screen placed as shown at the plane where a real image forms on the other side of the lens, the image of the opening will appear as



- A classical ideal gas, consisting of N particles $(N \to \infty)$ is confined in a box of volume V at temperature T and pressure p. The probability that, at any instant of time, a small sub-volume v_0 becomes totally void (i.e. no particles inside), due to a spontaneous statistical fluctuation, is
- (b) $\exp\left(\frac{-Nv_0}{V}\right)$ (c) $\frac{v_0}{V} \exp\left(\frac{-pV}{NT}\right)$
- (d) $\frac{pv_0}{NT}$
- where $\varphi_n(x,t)$ is the eigen-tis shown below. Note



If, for this cycle, $\frac{T_2}{T_3} = \left(\frac{p_2}{p_3}\right)^x$, the $X = \frac{1}{\sqrt{2}}$ (a) $1 - \frac{1}{\sqrt{2}}$

(d) - 1 CLASSES THE OPTIMIST CLASSES

$$\frac{p_2}{p_3} \Big)^x, \text{ then}$$
(b) 0 (c) 1 (d) $-\frac{1}{\gamma}$
as the wave function,
$$\psi(x,t) = \frac{1}{5} \Big[3\varphi_0(x,t) - 2\sqrt{2}\varphi_1(x,t) + 2\sqrt{2}\varphi_2(x,t) \Big]$$

wave function, $\psi(x,t) = \frac{1}{5} \left[3\varphi_0(x,t) - 2\sqrt{2}\varphi_1(x,t) + 2\sqrt{2}\varphi_2(x,t) \right]$ Enfunction belonging to the m^{th} energy $e^{\frac{1}{2}}$ where $\varphi_n(x,t)$ is the eigenfunction belonging to the n^{th} energy eigenvalue $\left(n+\frac{1}{2}\right)\hbar\omega$. The expectation value $\langle E\rangle$ of energy for the state $\psi(x,t)$ is (a) $1.58\hbar\omega$ (b) $0.46\hbar\omega$ (c) $\hbar\omega$ An energy eigenstate of the Hydrogen atom has $t^{1/2}$.

$$\psi_{n,\ell,m}(\mathbf{r},\theta,\phi) = \frac{1}{81\sqrt{r}} \left(\frac{1}{a_0}\right)^{3/2} \sin\theta \cos\theta \exp\left[-\left(\frac{r}{3a_0} + i\phi\right)\right]$$

The principal (n), azimuthal (ℓ) and magnetic (m) quantum numbers corresponding to this wave function are

(a)
$$n = 3, \ell = 2, m = 1$$

(b)
$$n = 2, \ell = 1, m = 1$$

(c)
$$n = 3, \ell = 2, m = -1$$
 (d) $n = 2, \ell = 1, m = \pm$

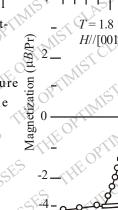
of PrGe is known to be 41 K. The magnet-ization of this sample is many ization of this sample is measured at 1.8

K for the magnetic field applied parallel

to the [001] direction is shown in the figure on the right. At a temperature of 38 K, the hysteresis loop in the figure will

(a) increase in width

(b) decrease in width



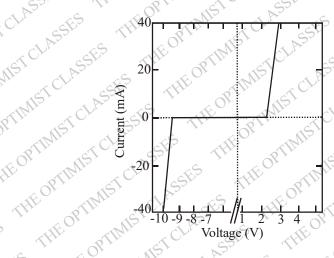
- (c) have the same width
- (d) shrink to a line

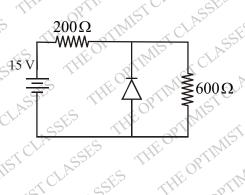
$$E_{\pm}=E_F\pm\Delta$$

Consider two energies of a free electron gas in a metal at an absolute temperature T, viz., $E_{\pm}=E_F\pm\Delta$ where E_F is the Fermi level. f the corresponding electron populations $n(E_{\pm})$ satisfy the relation $n(E_{\pm})$?

- (a) $k_B T_{\rm c}$

- $E_{\pm}=E_F\pm\Delta$ E_F is the Fermi level. If the corresponding electron populations $n(E_{\pm})$ satisfy the relation $n(E_{\pm})/n(E_{\pm})=2$, then $\Delta=$ (a) k_BT (b) $k_BT\ell n2$ (c) $\frac{k_BT}{2}$ (d) $2k_BT$ The figure on the right shows the current-voltage characteristics of a diode α where it is safe to operate the diode. The figure on the right shows the current-voltage characteristics of a diode over a range of voltage and current where it is safe to operate the diode.





When this diode is used in the circuit on the extreme right, the approximate current, in mA, through the diode will be will be (b)16.7

To be attempted only by candidates for Ph.D. programme.

The integral

egral
$$\int_{-\infty}^{\infty} dx \delta(x^2 - \pi^2) \cos x$$
 es to

evaluates to

(c)
$$-\frac{1}{\pi}$$

(d)
$$\frac{1}{\pi}$$

If z = x + iy then function

waluates to

(a) - 1

(b) 0

(c)
$$-\frac{1}{\pi}$$

(d) $\frac{1}{\pi}$

(e) $\frac{1}{\pi}$

(f) $\frac{1}{\pi}$

(f) $\frac{1}{\pi}$

(g) $\frac{1}{\pi}$

(here a is a real parameter, is analytic in the complex z plane if $a = a$

(here $a = a$

$$(b) + 1$$

A particle of mass m moves in one dimension under the influence of a potential energy $V(x) = -a^{-1/2} \cdot (x)^{\frac{1}{4}}$

$$V(x) = -a\left(\frac{x}{l}\right)^2 + b\left(\frac{x}{l}\right)^4$$

where a and b are positive constants and l is a characteristic length. The frequency of small oscillations

about a point of stable equilibrium is

(a)
$$\frac{1}{2\pi l} \sqrt{\frac{b}{m}}$$

(b)
$$\frac{1}{\pi l} \sqrt{\frac{a^2}{mb}}$$

(c)
$$\frac{2b}{\pi l} \sqrt{\frac{1}{ma}}$$

(d)
$$\frac{1}{\pi l} \sqrt{\frac{a}{m}}$$

If a central force acting on a particle of mass m is given by

$$F(r) = \frac{k}{r^2}$$

Where r is the distance of the particle from the origin and k is a positive constant, the Hamiltonian for the system, in spherical polar coordinates will have the form system, in spherical polar coordinates, will have the form

(a)
$$\frac{1}{2}m(\dot{r}^2 + r^2\dot{\theta}^2 + r^2\sin^2\theta\dot{\varphi}^2) + \frac{k}{r}$$

(b)
$$\frac{1}{2mr^2} \left(r^2 p_r^2 + p_\theta^2 + p_\varphi^2 + 2mkr \right)$$

(c)
$$\frac{p_r^2}{2m} + \frac{p_\theta^2}{2mr^2} + \frac{p_\phi^2 \cos ec^2 \theta}{2mr^2} + \frac{k}{r}$$

(d)
$$\frac{p_r^2}{2m} + \frac{p_\theta^2}{2m} + \frac{p_\varphi^2}{2m} + \frac{k}{r}$$

(a) $\frac{1}{2}m(\dot{r}^2 + r^2\dot{\theta}^2 + r^2\sin^2\theta\dot{\varphi}^2) + \frac{k}{r}$ (b) $\frac{1}{2mr^2}(r^2p_r^2 + p_\theta^2 + p_\varphi^2 + 2mkr)$ (c) $\frac{p_r^2}{2m} + \frac{p_\theta^2}{2mr^2} + \frac{p_\varphi^2\cos ec^2\theta}{2mr^2} + \frac{k}{r}$ (d) $\frac{p_r^2}{2m} + \frac{p_\theta^2}{2m} + \frac{p_\varphi^2}{2m} + \frac{k}{r}$ Q45. The magnetic vector potential $\vec{A}(\vec{r})$ corresponding to a uniform magnetic field \vec{B} is taken in the form

$$\vec{A} = \frac{1}{2}\vec{B} \times \vec{r}$$

where ω is a constant, the gauge choice corresponding to this potential is a (a) non-linear gauge (b) Lorentz gauge (c) time - varying gauge where \vec{r} is the position vector. If the electric field has the time - dependent form

$$\vec{E} = \vec{E}_0(\vec{r})e^{i\omega t}$$

(a) non - linear gauge

- A binary star is observed to consist of a blue star B (peak wavelength 400 nm) and a red star R (peak wavelength 800 nm) orbiting each other. As observed from the Earth, B and R appear equally bright. As-

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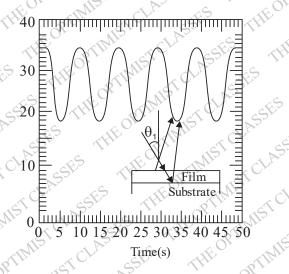
	(a) 64 (b) 1/64 (c) 16 (d) 1/16
Q47	A system at temperature T has three energy states $0, \pm \varepsilon$. The entropy of the system in the low temperature
è	$(T \to 0)$ and high temperature $(T \to \infty)$ limits are, respectively,
SSES	(a) $S_{T\to 0} = 0$ and $S_{T\to \infty} = k_B \ln 3$ (b) $S_{T\to 0} = 0$ and $S_{T\to \infty} = k_B \ln 3$
155	(c) $S_{T\to 0} = 0$ and $S_{T\to \infty} = \kappa_B \exp(-S)$ (d) $S_{T\to 0} = 0$ and $S_{T\to \infty} = S\kappa_B + Z$
Q48	The state $ \psi\rangle$ of a quantum mechanical system, in a certain basis, is represented by the column vector
IST CL	The state $ \psi\rangle$ of a quantum mechanical system, in a certain basis, is represented by the column vector $ \psi\rangle = \begin{pmatrix} 1/\sqrt{2} \\ 0 \\ 1/\sqrt{2} \end{pmatrix}$ The operator \hat{A} corresponding to a dynamical variable A , is given, in the same basis, by the matrix $\begin{pmatrix} 1 & 1 & 1 \end{pmatrix}$
OPTI	The operator \hat{A} corresponding to a dynamical variable A , is given, in the same basis, by the matrix
jt.	The operator \hat{A} corresponding to a dynamical variable A , is given, in the same basis, by the matrix $\hat{A} = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 2 & 1 \\ 1 & 1 & 2 \end{pmatrix}$ If, now, a measurement of the variable A is made on the system in the state $ \psi\rangle$, the probability that the result will be $+1$ is (a) $\frac{1}{4}$ (b) $\frac{1}{\sqrt{2}}$ (c) $\frac{1}{2}$ (d) 1 A spin- $\frac{1}{2}$ particle A decays to two other particles B and C . If B and C are of spin- $\frac{1}{2}$ and spin-1 respectively, then a complete list of the possible values of the orbital angular momentum of the final state (i.e. $B + C$) is
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	HIE OPTIMITES CLAR SSES (THE 2) TIME STOLAR SSES THE OF SPIRMES OF CLARE
SES .	If, now, a measurement of the variable A is made on the system in the state $ \psi\rangle$, the probability that the result
SSE	will be #1 is 27 that GLAS SES THE OF THAT STIMES
LAS	SES 1 THEOR DIMINES TOLAS SES THEOR THIS COLAS (A) THEOR THIS
CLA	If, now, a measurement of the variable A is made on the system in the state $ \psi\rangle$, the probability that the result will be ± 1 is (a) $\frac{1}{4}$ (b) $\frac{1}{\sqrt{2}}$ (c) $\frac{1}{2}$ (d) 1 A spin- $\frac{1}{2}$ particle A decays to two other particles B and C . If B and C are of spin- $\frac{1}{2}$ and spin-1 respectively,
ο Q49ς (A spin- $\frac{1}{2}$ particle A decays to two other particles B and C. If B and C are of spin- $\frac{1}{2}$ and spin-1 respectively,
IMIS.	then a complete list of the possible values of the orbital angular momentum of the final state (i.e. $B+C$) is
TIM	(a) $0, 1$ (b) $\frac{1}{2}, \frac{3}{2}$ (c) $0, 1, 2$ (d) $0, \pm 1$
Ob	AND CON SEE ART ON IS THE TONK OF IS
Q50.	When a pure element is vaporised and placed in a uniform magnetic field B_0 , it is seen that a particular spectral
	line of wavelenght λ , corresponding to a $J=1 \rightarrow J=0$ transition, gets split into three components $\lambda, \lambda \pm \Delta \lambda$.
S (1)	It follows that the Lande g-factor for the transition $J = 1 \rightarrow J = 0$ is given by
, ,5	(a) $g = \frac{hc}{\mu_B B_0} \frac{\Delta \lambda^2}{\lambda}$ (b) $g = \frac{hc}{\mu_B B_0} \frac{\Delta \lambda}{\lambda^2}$ (c) $g = \frac{hc}{\mu_B B_0} \frac{\lambda^2}{\Delta \lambda}$ (d) $g = \frac{hc}{\mu_B B_0} \frac{\lambda}{\Delta \lambda^2}$
SSE	$\mu_B D_0 \wedge \mu_B $
Q515	The rate of deposition of a dielectric thin flim on a thick dielectric substrate was monitored by the following experiment:
, (d	a laser beam of wavelength $\lambda = 633\mathrm{nm}$, at near-normal incidence θ_r , was reflected from the thin flim (see
MSI	inset figure on the right), and the reflection coefficient R was measured. As the film thickness increased R varied with time as shown in the figure. The refractive index of the substrate. Using the graph, the approximate thickness of the film at the end of 25 seconds can be estimated to be
BIL	(a) $0.017 \mu m$ (b) $0.51 \mu m$ (c) $0.26 \mu m$ (d) $2.2 \mu m$
TE OPT	MISTO CLASSE THE OPTIMALISTON ASSESSED THE OPTIMAL ASSESSED
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(c) 16

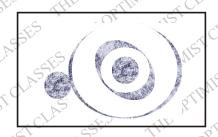
stars is (a) 64

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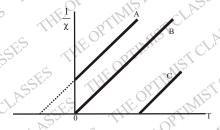
THE OPTIMIST CT



The negative image on the right represents a very small portion of the night sky at a very high resolution. Notice the broken ring(s) around the central bright object in the middle of the picture. These are most likely to be due



- (a) gravitational lensing of a distant object by the central massive object
 (b) gas clouds forming the remnant of a supernova explosion
 (c) debris from a smaller object form
- (c) debris from a smaller object torn apart by tidal forces
- (d) ice collected on the lens used for taking the picture
- THE OF Q53. The magnetic susceptibility χ of three sample A,B and C, is measured as a function of their absolute temperature T leading to the sample Ature T, leading to the graphs shown below.



From these graphs, the magnetic nature of the samples can be inferred to be

(a) A: anti-ferromagnet

B: diamagnet

(b) A: diamagnet

B: paramagnet

C: anti-ferromagnet

(c) A: paramagnet

B: anti-ferromagnet

C: ferromagnet

(d) A: anti-ferromagnet

B: paramagnet

C: ferromagnet

A gold foil, having N(0) number of ¹⁹⁷ Au nuclides per cm², is irradiated by a beam of thermal neutrons with a As a result, the nuclide 198 Au, with a half-life τ of several years, is produced by flux of F neutrons- cm^{-2} - s^{-1} . the reaction

$$^{197}\mathrm{Au} + n \rightarrow ^{198}\mathrm{Au} + \gamma$$

Au nuclides, the conal to (d) $\sigma \tau FN(0)$ Which has a cross section of σ cm². Assuming that the gold foil has 100% abundancy of ¹⁹⁷Au nuclides, the maximum number of ¹⁹⁸Au nuclides that can accumulte at any time in the foliation. THE OPTIMIST CLASSES THE OPTIMIST CLASSES maximum number of 198 Au nuclides that can accumulte at any time in the foil is proportional to

(a)
$$\frac{\sigma F}{\tau}N(0)$$

(b)
$$\frac{1}{\sigma \tau F} N(0)$$

(c)
$$\frac{\tau}{\sigma F}N(0)$$

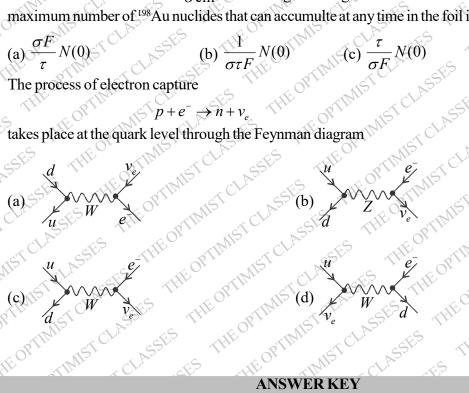
(d)
$$\sigma \tau FN(0)$$

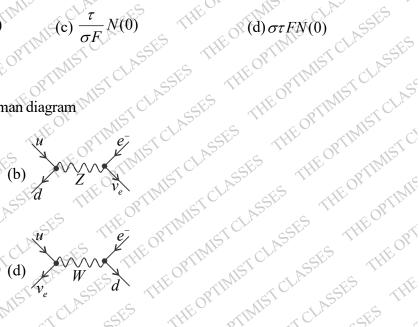
THE OPTIMIST CLASSES THE OPTIMIST C

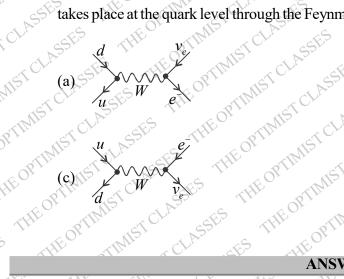
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THE OPTIMIST CLASSE

$$p + e^- \rightarrow n + v$$







$$\begin{array}{c} (b) \\ Z \\ v_e \\ \end{array}$$

$$(d) \\ v_e \\ W \\ d \\ \end{array}$$
ANSWER KEY

ANSWER KEY

- (a) (b) THE OPTIMES TOL 2;MIS 9. 5 (d) 4.0P (c) 115° (a) 3. (b) 5. 6. (b) 55¹ (c,d) (a) (a) SSES THE OPTIMIST CLA OPTIMISTOLAS 10 10. 12. (a) 14. 16. (c) **Q**5. (d) **17**. (a) 18.5 THE OPTIMIST CLASSES THE OPTIM (d) 20. 24. (a) 21. (d) 22. (d) 23. (b) 25.5 26. (d) (a) FLOT (c) 32. (c) 37. (c) 38. (b)
 - THE OPTIMIST CLASSES THE OPTIMIST CLASSES THE OPTIMIST CLASSES (a) S. THE OPTIMIST CLASSES TH 31. 43. THE OPTIMIST CLASSES THE OPTIMIST CLASSES 44.
 (c) 50.
 (c) 45. 46.
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 - (d, 55, 5) (c) THE OPTIMIST CLASSES